

"How Strange is the Proton?

Neutrinos DIS and the Strange Quark Asymmetry

A collection of interesting puzzles

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SMU

LANL P- 25 Seminar
7 September 2005

Why are we interested in the Proton structure?

* Because it's there!

What is the structure of hadrons?

What is the character of the QCD theory?

... the other forces are comparatively weak

* Because we need this information

for any hadron- induced process.

Compare these machines:

LEP e^+e^- $\sqrt{s} = 200 \text{ GeV}$

HERA ep $\sqrt{s} = 314 \text{ GeV}$

RHIC NN $\sqrt{s} = N \times 100 \text{ GeV}$

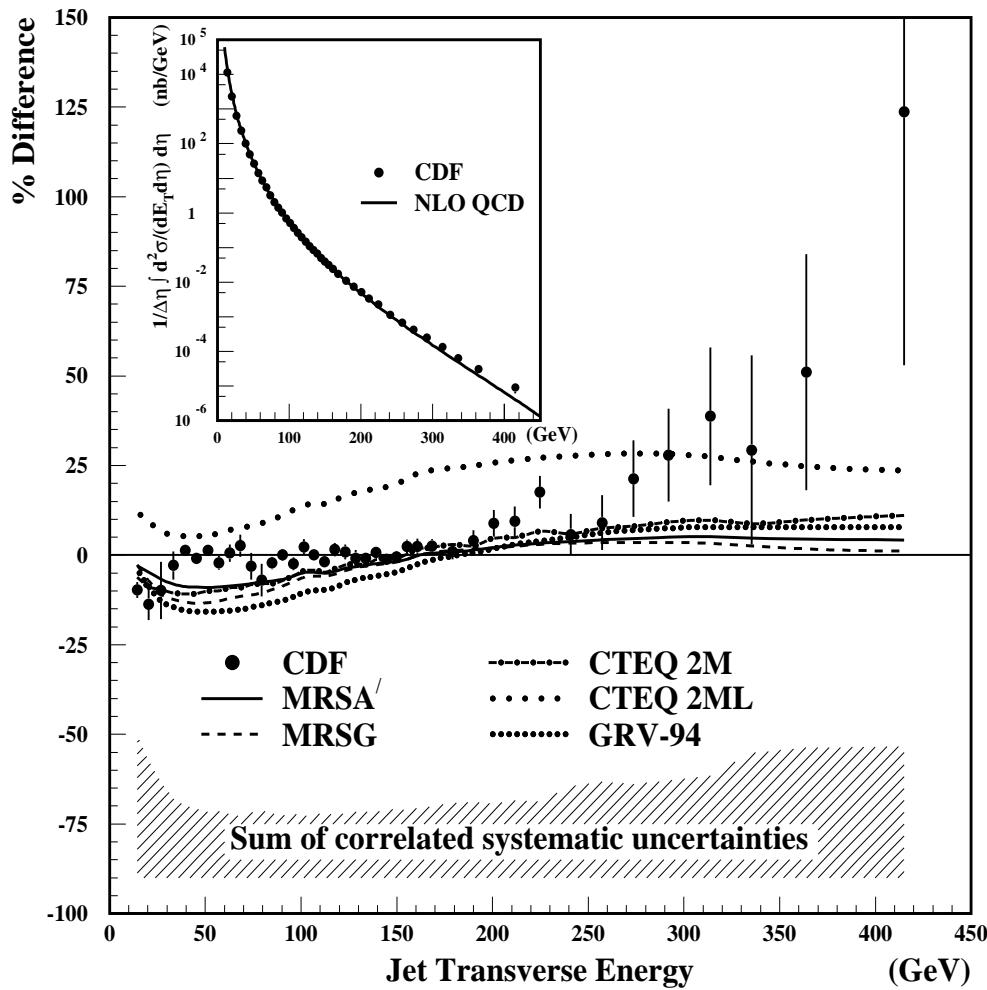
Tevatron $p - p - \bar{p}$ $\sqrt{s} = 2000 \text{ GeV}$

LHC pp $\sqrt{s} = 14,000 \text{ GeV}$

The Search For New Physics

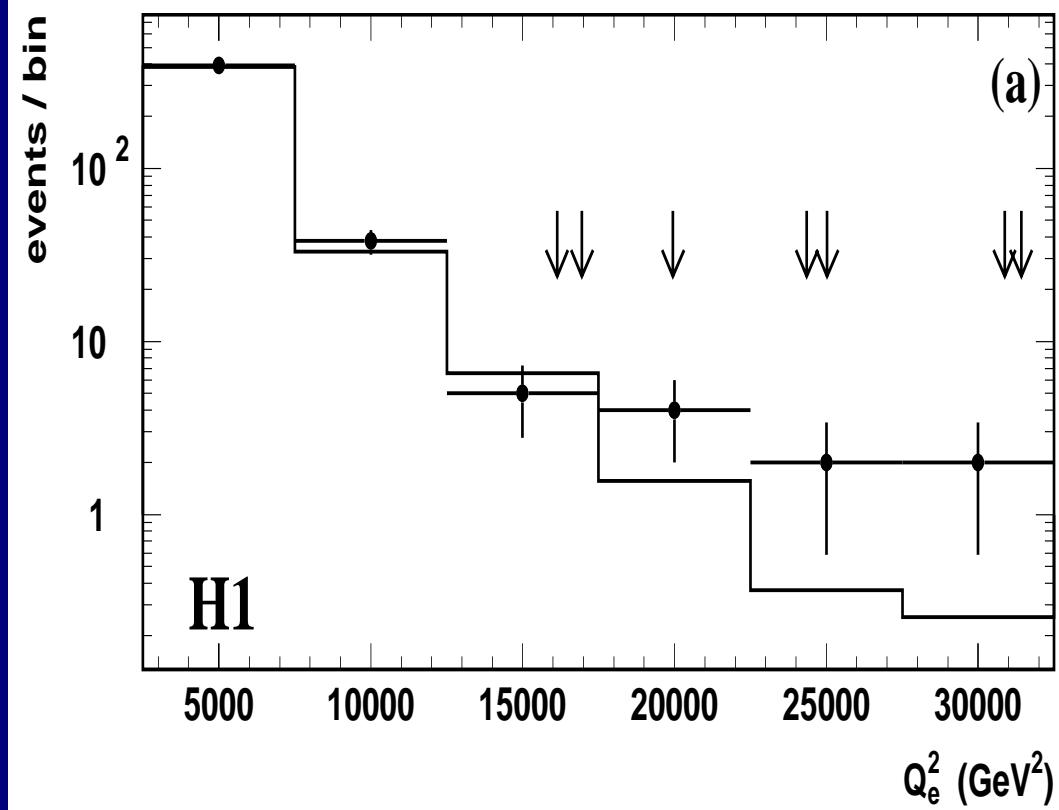
1996: Excess High E_T Jets at Tevatron

Is this a sign of compositeness?



CDF Collaboration
PRL 77, 438 (1996)

1997: Excess DIS events at large $\{x, Q^2\}$
Is this a sign of lepto-quarks?

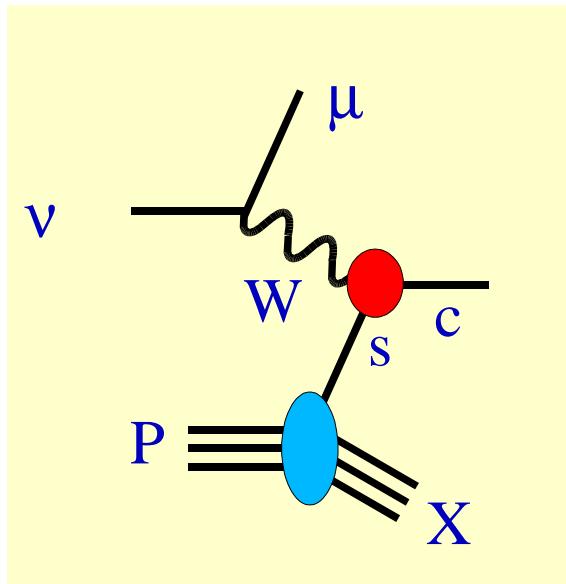


H1 Collaboration, ZPC74, 191 (1997)
ZEUS Collaboration, ZPC74, 207 (1997)

Precision PDF's are essential

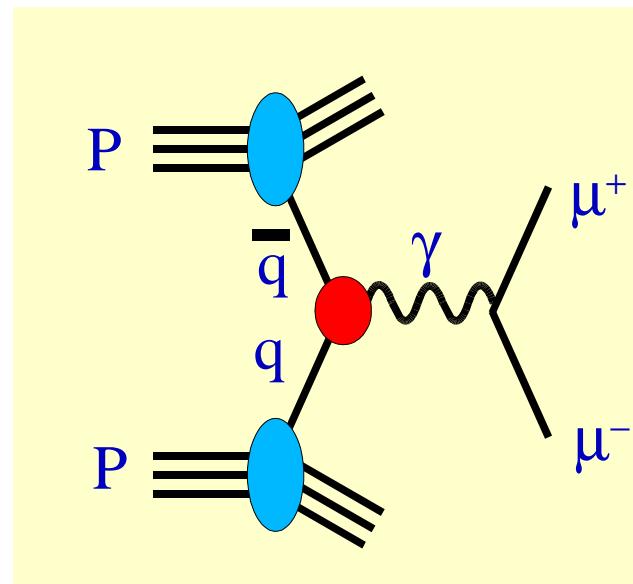
The Basic Processes

Deeply Inelastic Scattering (DIS)



$$\sigma_{DIS} = f_{P \rightarrow s} \otimes \hat{\sigma}_{s \rightarrow c}$$

Drell- Yan (DY)



$$\sigma_{DY} = f_{P \rightarrow q} \otimes f_{P \rightarrow \bar{q}} \otimes \hat{\sigma}_{q\bar{q} \rightarrow \mu^+ \mu^-}$$

Use data to extract PDF, then make predictions for other processes

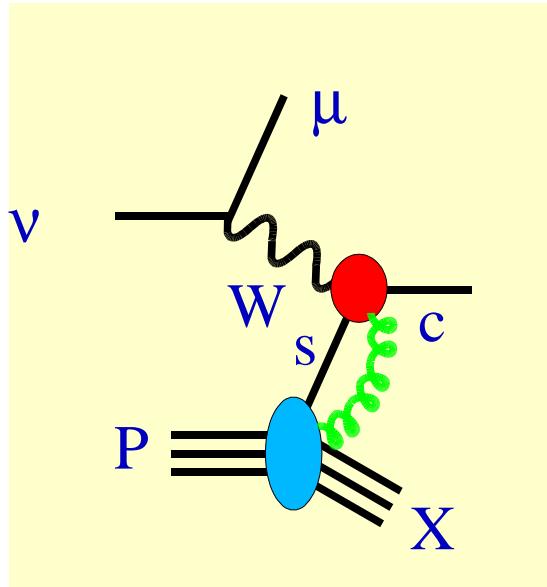
Factorization: Convolution of independent probabilities

$\tau_{INT} < \tau_{HAD}$: If $\tau_{INT} \sim 1/Q$ and $\tau_{HAD} \sim 1/M$, then $\Rightarrow Q/M > 1$

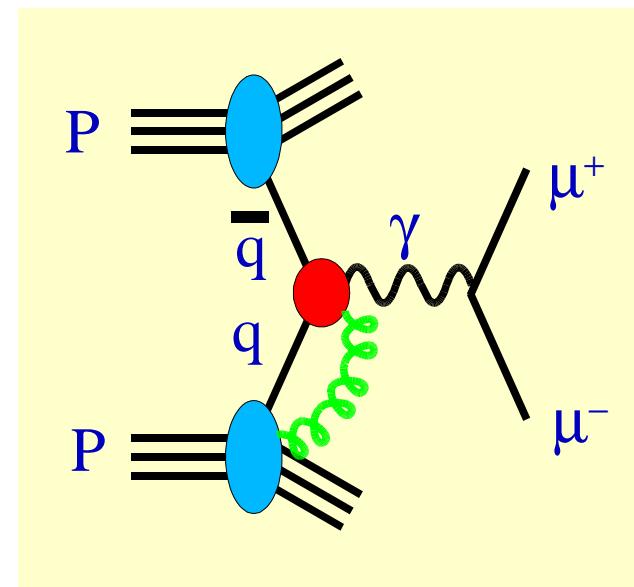
What if $Q/M \leq 1$??? Higher Twist

What about Higher Twist???

Deeply Inelastic Scattering (DIS)



Drell- Yan (DY)

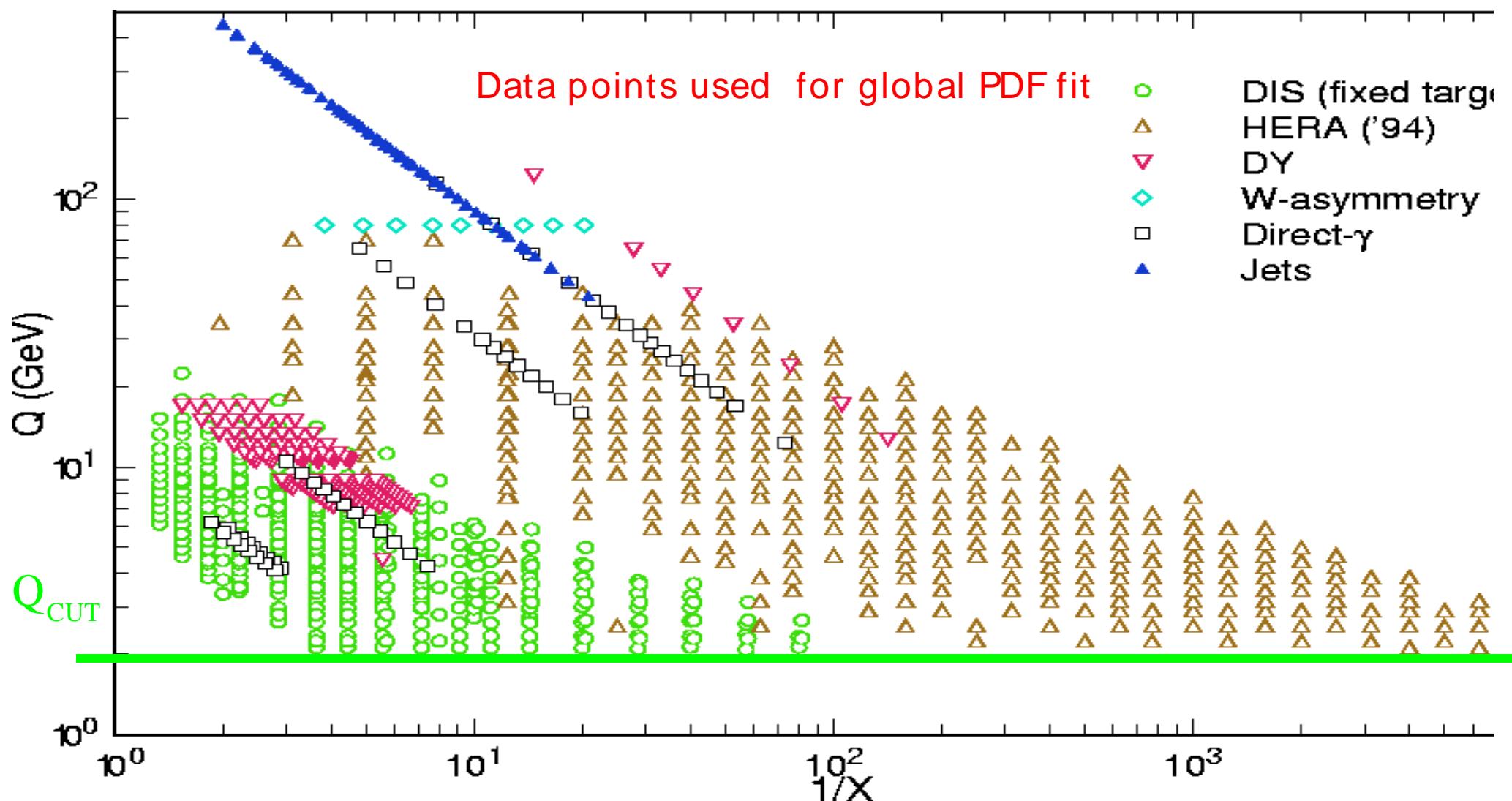


$$\sigma_{DIS} = \cancel{f_{P \rightarrow s}} \otimes \hat{\sigma}_{s \rightarrow c}$$

$$\sigma_{DY} = f_{P \rightarrow q} \otimes \cancel{f_{P \rightarrow \bar{q}}} \otimes \hat{\sigma}_{q\bar{q} \rightarrow \mu^+ \mu^-}$$

- Factorization breaks down
- Lose Universality
- No “First Principles” model
... sometimes parameterized as a $1/Q^2$ correction

What data are used in global fit to extract PDF's

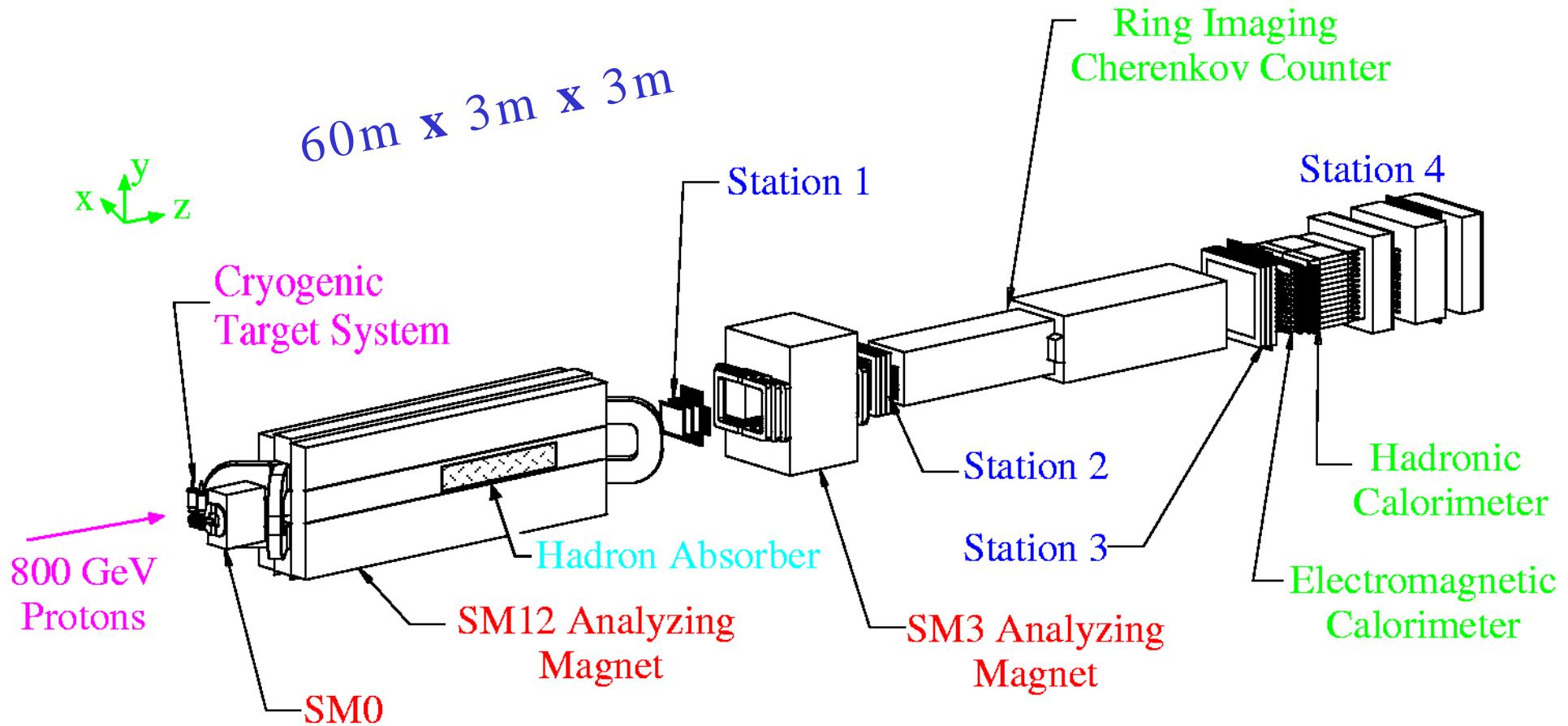


- * Precision data essential to PDF, and hence, "new physics" searches
- * **Both** Fixed Target and Collider data needed to map out full $\{x, Q\}$ space
- * Note "cuts" in $\{x, Q\}$ space; many data points outside these cuts

Moral

Extended theoretical understanding of the “higher twist” region would allow us to include the wealth of data available in this region.

DrellYan: Fermilab E866/ NuSea Detector

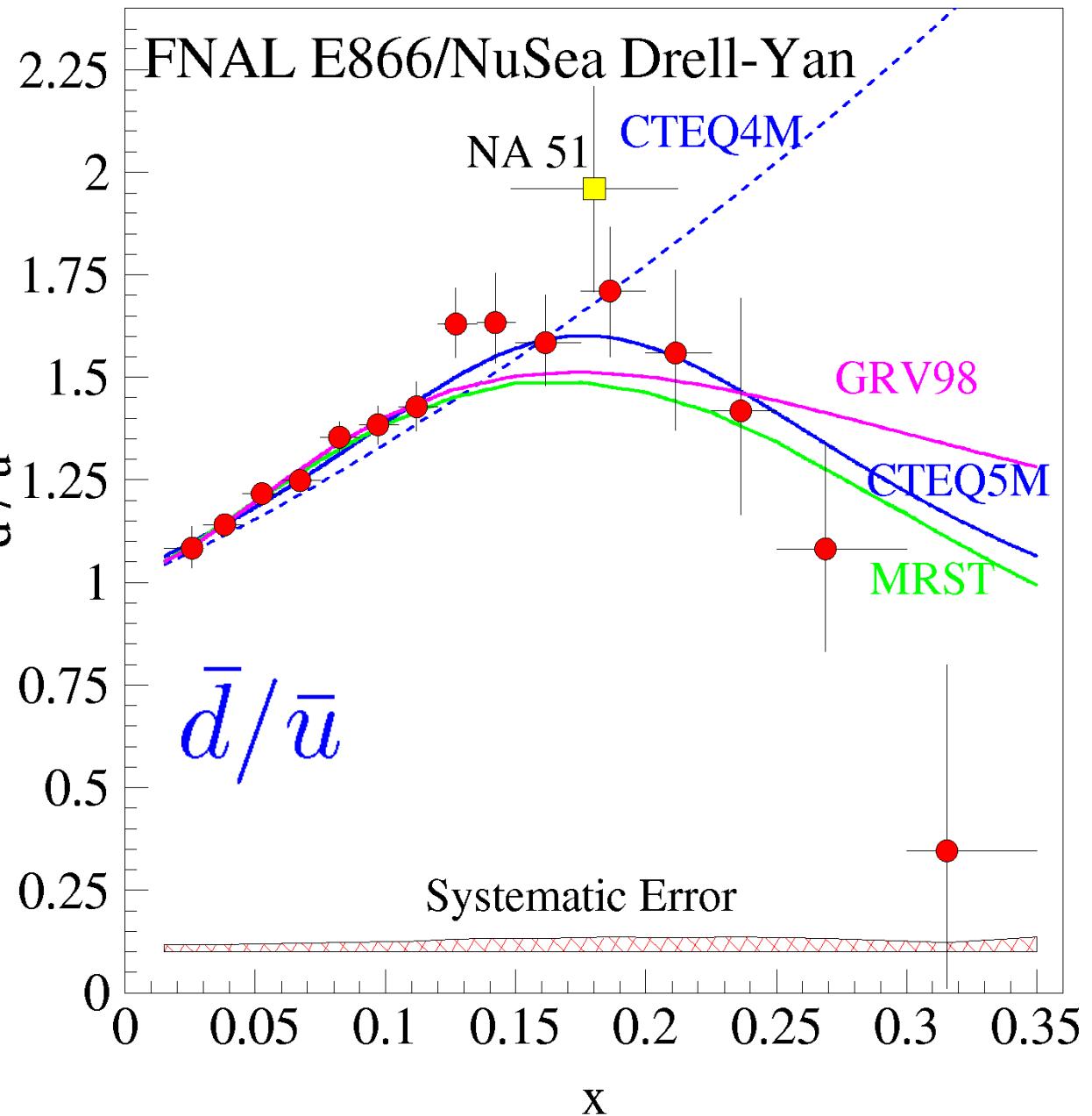


- Forward x_P high mass μ - pair spectrometer
- Liquid hydrogen and deuterium targets
- Two acceptance defining magnets (SM0, SM12)
- Also used solid W, Be, Fe targets
- Beam dump (4.3m Cu)
- Hadronic absorber (13.4 I₀- Cu, C, CH₂)
- Momentum analyzing magnet (SM3)
- Three tracking stations
- Muon identifier wall & 4th tracking

E866 quark sea distributions:

Examine ratio of deuterium to hydrogen

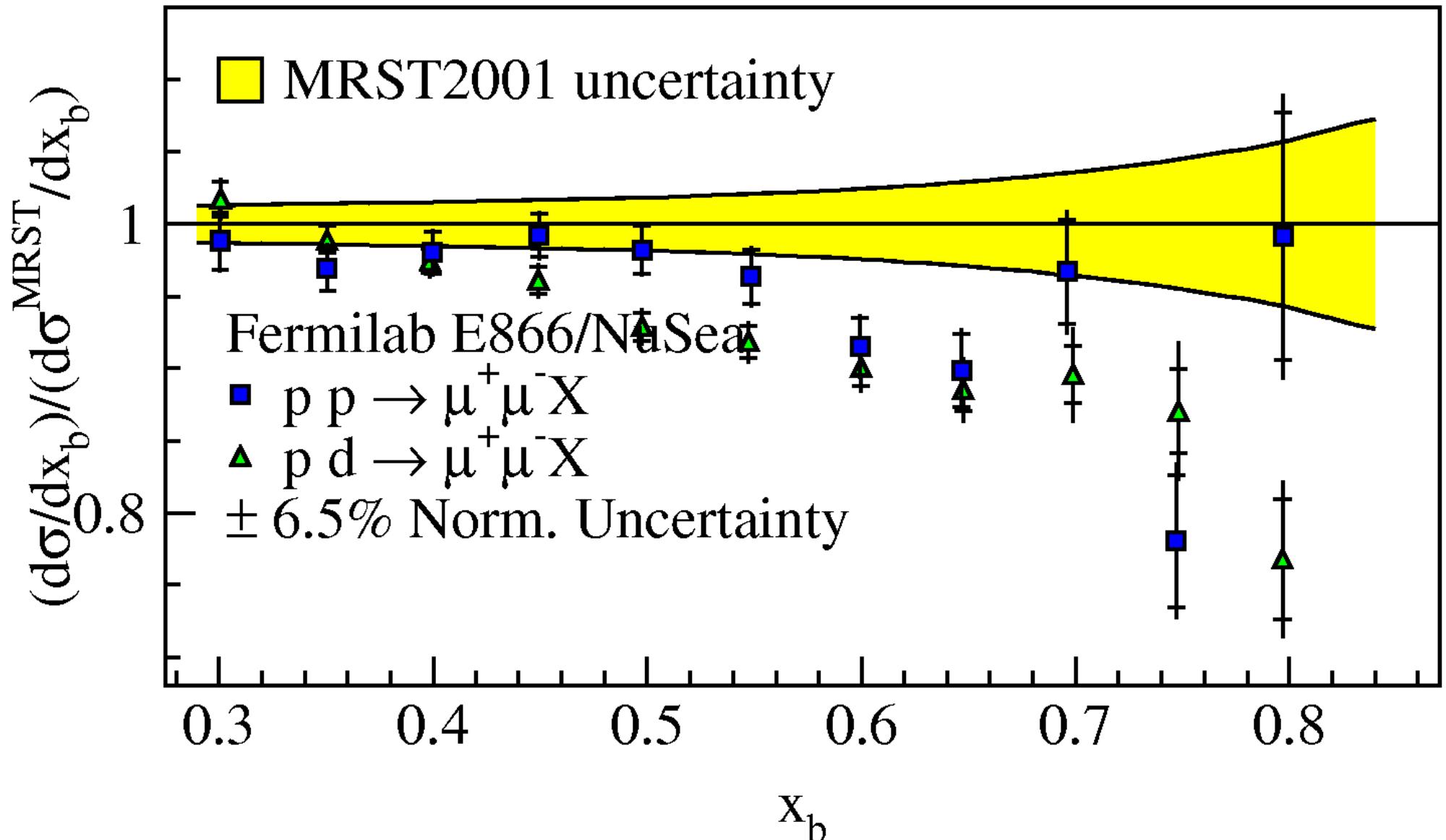
$$\frac{\sigma^{pd}}{2\sigma^{pp}} \Big|_{x_b \gg x_t} \approx \frac{1}{2} \left[1 + \frac{\bar{d}(x_t)}{\bar{u}(x_t)} \right]$$



Even for a “mature” analysis,
new data can have a large impact

Donald Isenhower (ACU)
DIS'04

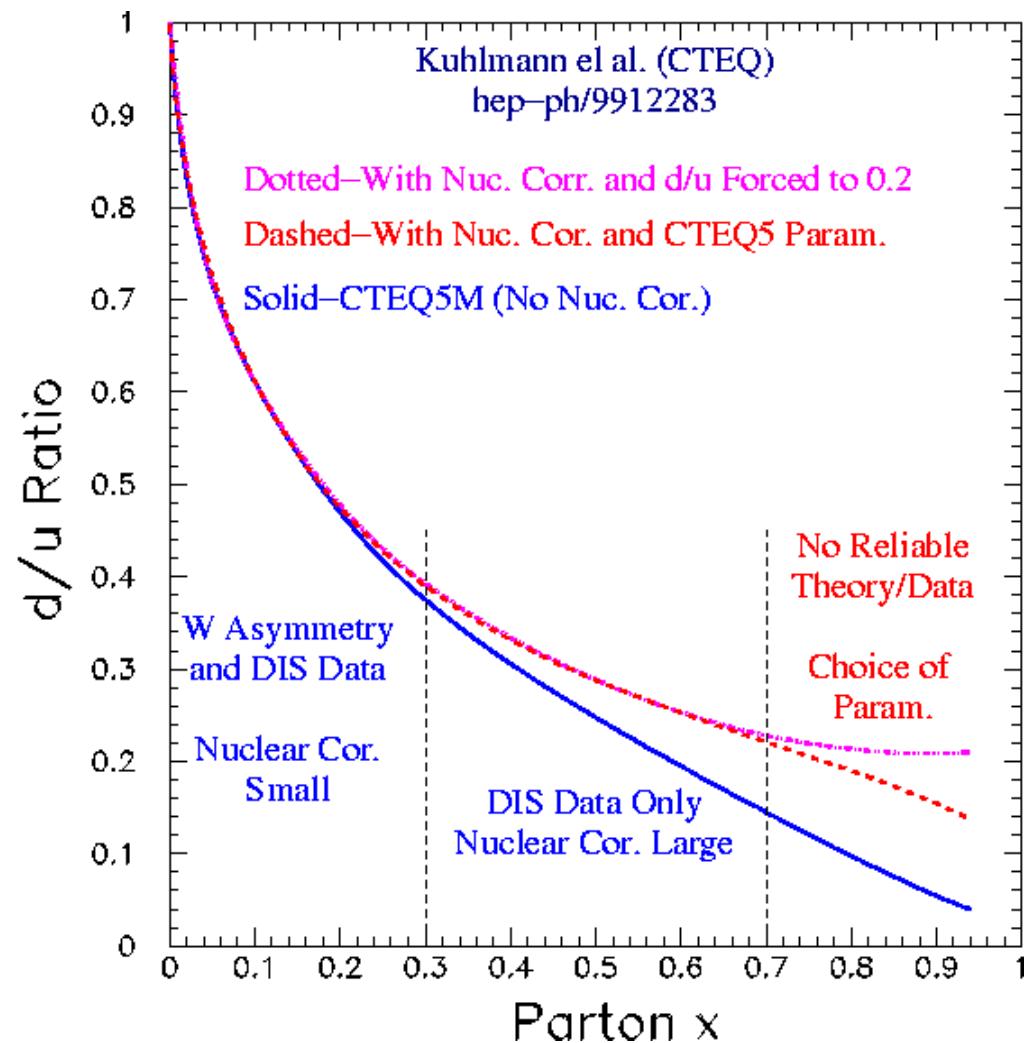
Drell- Yan Cross Section in large x limit



$d\sigma \sim (4 u + d)$ in large x limit

Theory over estimates data in this limit

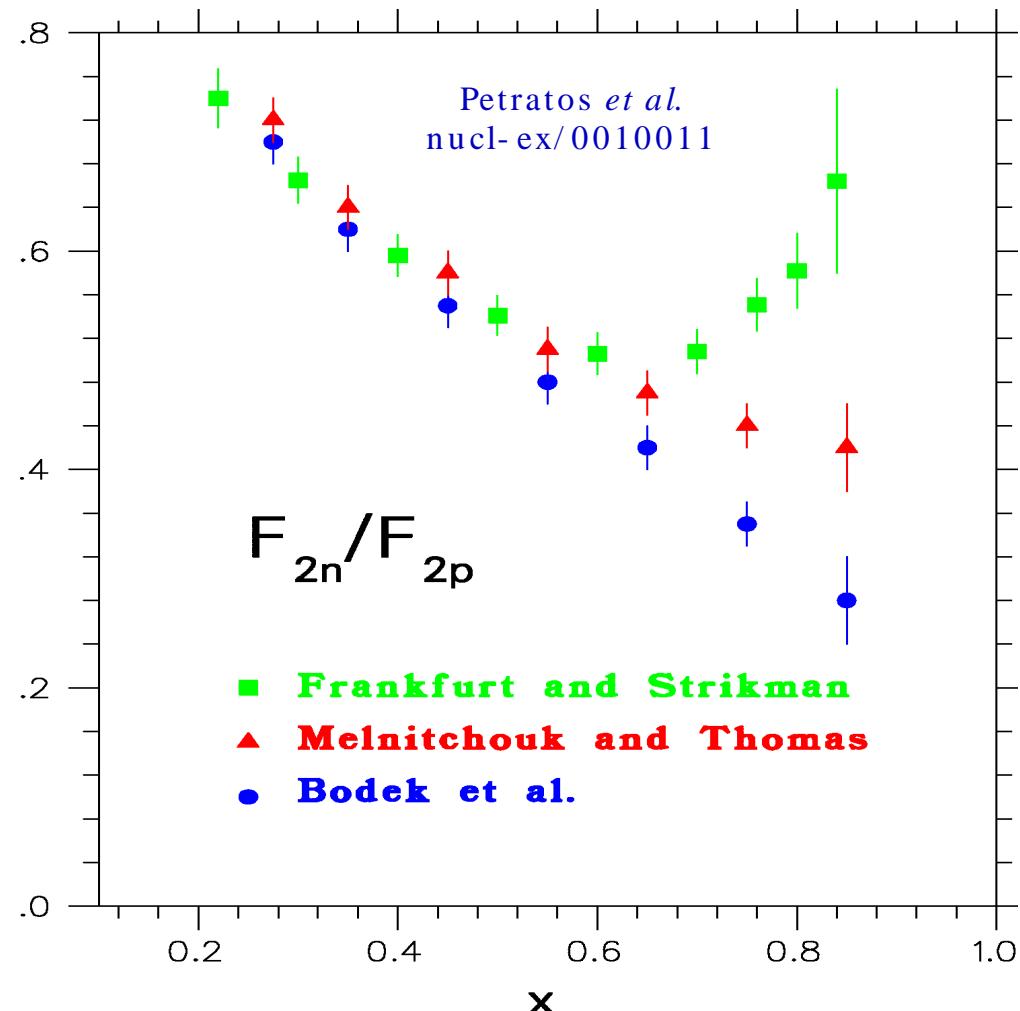
Proton Valence Structure: d/u for large x



For large x, nuclear binding/Fermi motion corrections are important

Even Deuteron has large effects

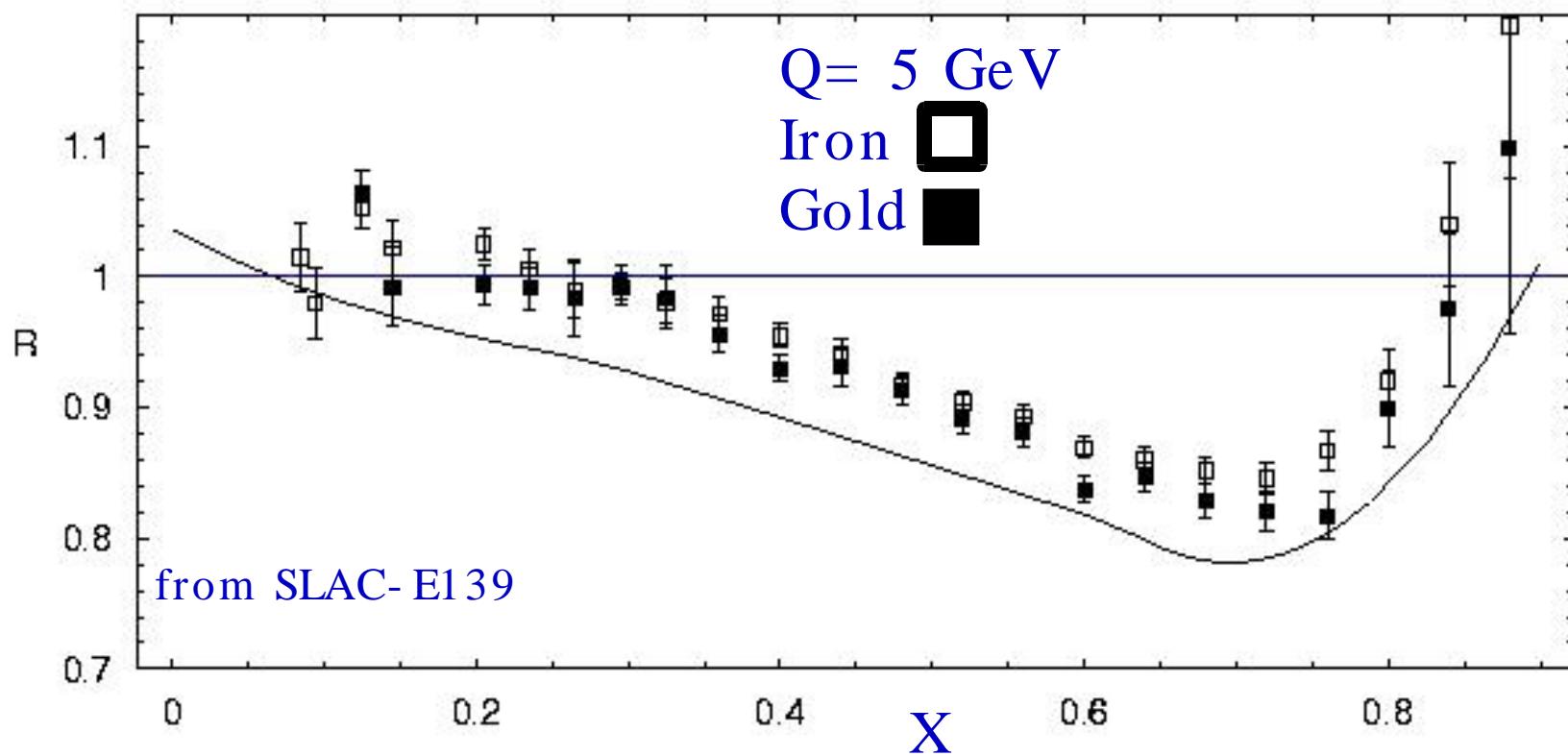
Lots of models to choose from



Is a Hadron simply a sum of its parts? The EMC Effect

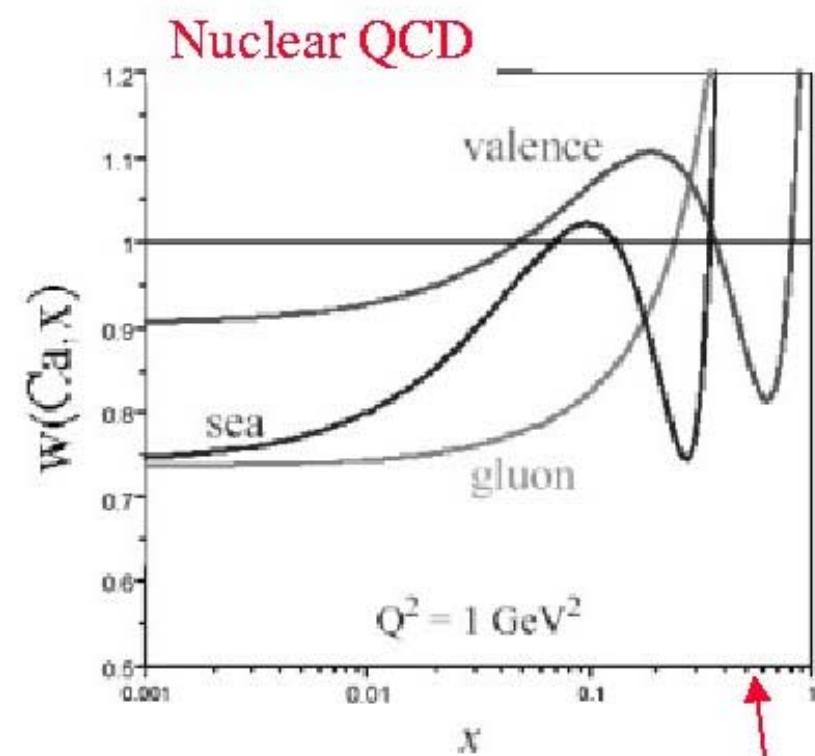
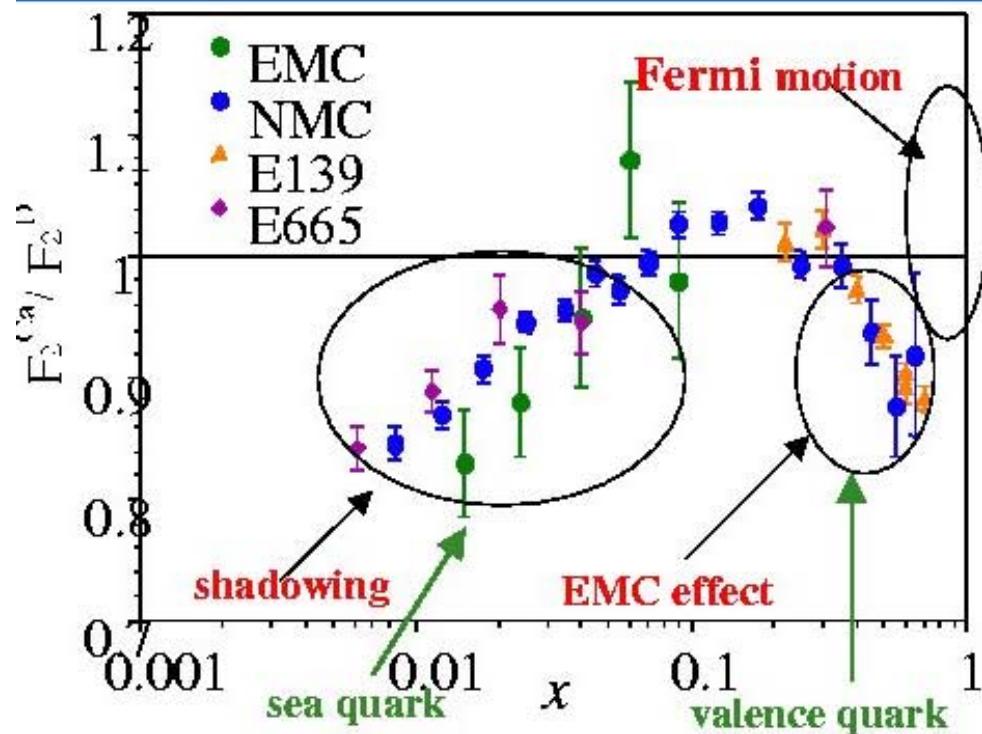
$$R(x, Q) = \frac{F_2^A(x, Q)}{A F_2^N(x, Q)}$$

Measures the extent to which nuclei are not a Σ of free nucleons



We're simplifying parameterizing our ignorance

Knowledge of Nuclear Effects with Neutrinos: essentially NON-EXISTENT



$F_2 / \text{nucleon}$ changes as a function of A . Measured in $\mu/e - A$ not in $\nu - A$

Good reason to consider nuclear effects are DIFFERENT in $\nu - A$.

- ▼ Presence of axial-vector current.
- ▼ **SPECULATION:** Much stronger shadowing for $\nu - A$ but somewhat weaker “EMC” effect.
- ▼ Different nuclear effects for valance and sea \rightarrow different shadowing for xF_3 compared to F_2 .
- ▼ Different nuclear effects for d and u quarks.



Assume 4.0×10^{20} in LE ν beam, 8×10^{20} in ME, 1.5×10^{20} in HE and 2.5×10^{20} in HEbar

ν_μ Event Rates in 3 fiducial tons of CH

Process	CC	NC	CCbar
Quasi-elastic	835 K	275 K	105 K
Resonance	1605 K	495 K	130 K
Transition	2000 K	635 K	230 K
DIS	4080 K	1215 K	455 K
Coherent	85 K	43 K	20 K
TOTAL	8600 K	2665 K	940 K

Typical Fiducial Volume =
 3-5 tons CH, 0.6 ton C, \approx 1 ton Fe
 and \approx 1 ton Pb

8.6 - 14.3 M ν events in CH
1.0 - 1.5 M $\bar{\nu}$ events in CH
1.4 M ν events in C
2.9 M ν events in Fe
2.9 M ν events in Pb

16 Million total CC events in a 4 - year run

Examples of available statistics

Transition Region

2 M events

DIS and Structure Functions

4 M DIS events ($W > 2$, $Q > 1$)

Nuclear PDF's and Effects

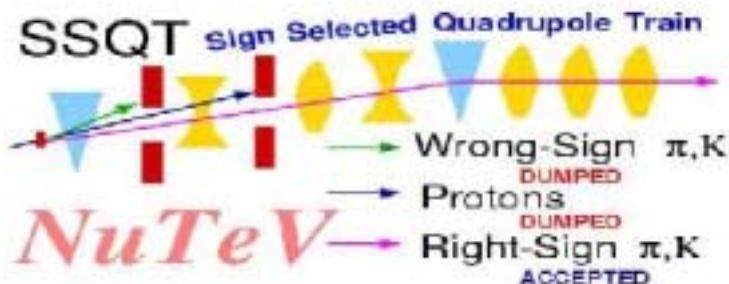
C:1.4 M, Fe: 2.9 M and Pb: 2.9 M

For the global analysis,
we prefer to reduce nuclear
data
to the isoscalar case;
but this reduction is not
trivial

Let's turn to Neutrino- Induced DIS

The NuTeV experiment at FNAL

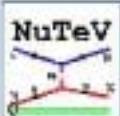
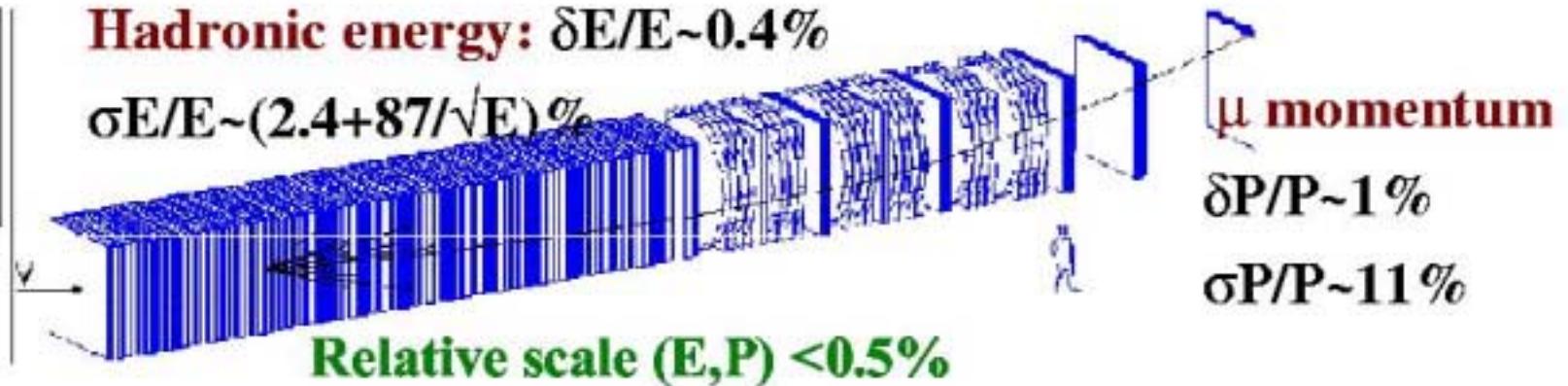
ν -N DIS, sign-selected beam $\langle E_\nu \rangle \sim 120$ GeV
and continuous test beam calibration



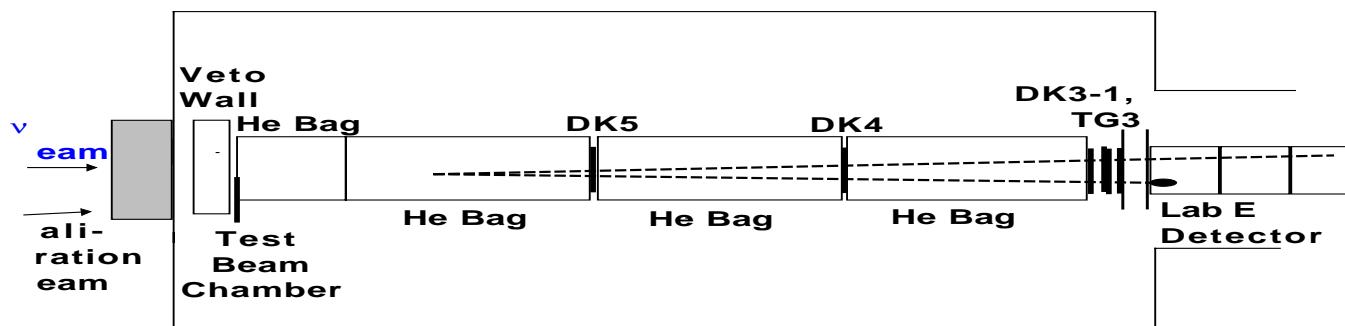
Data taken
during
1996-97

Hadronic energy: $\delta E/E \sim 0.4\%$

$$\sigma E/E \sim (2.4 + 87/\sqrt{E})\%$$



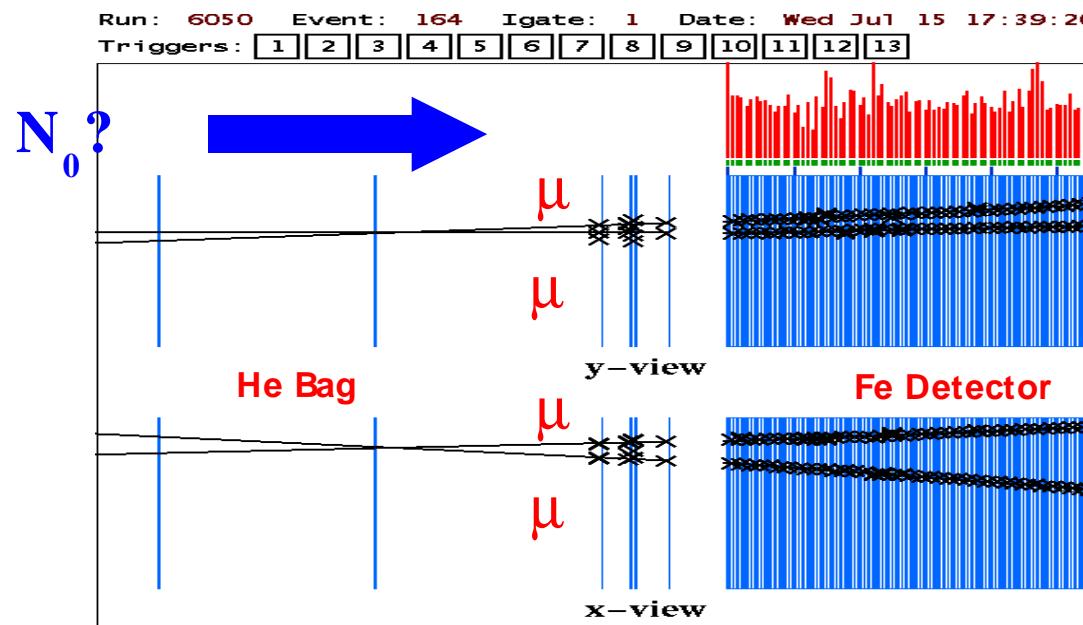
Anomalous $\mu\mu$ events in Neutrino- Induced DIS



Todd Adams
NuTeV Collaboration
PRL 87:041801 (2001)

Could this be evidence for an heavy neutral lepton?

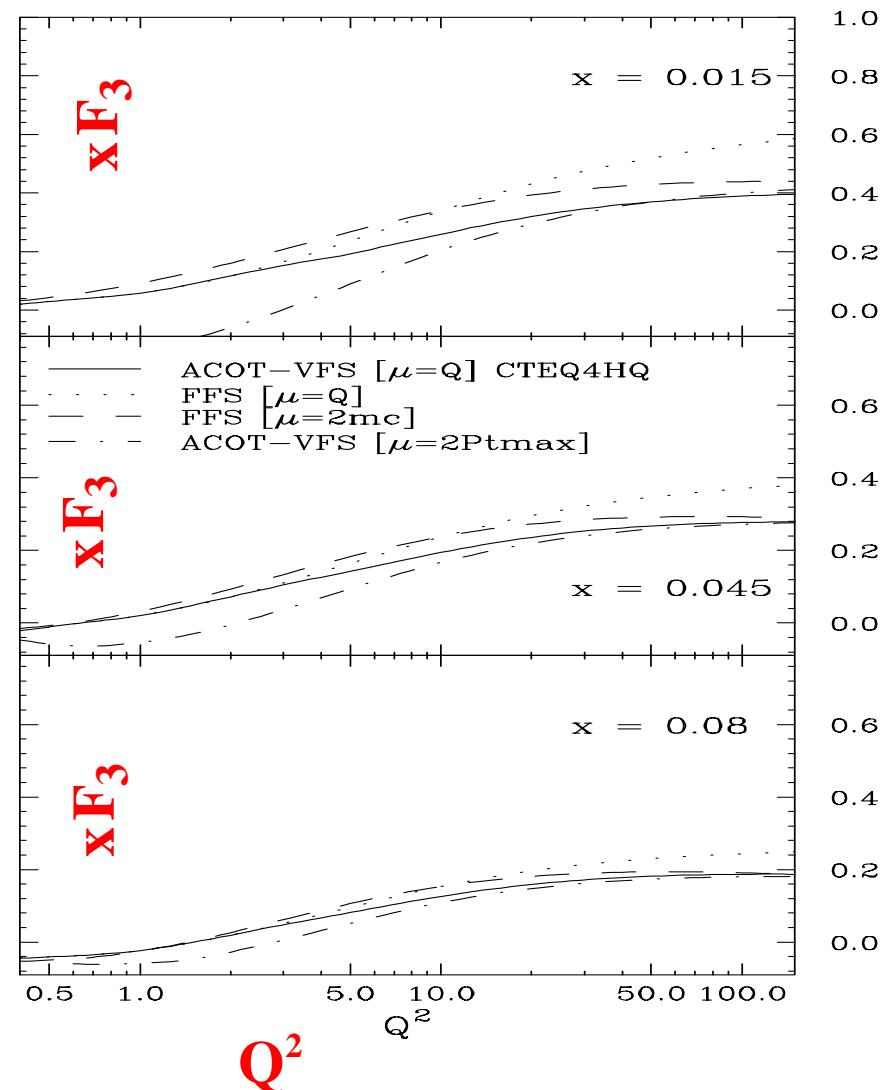
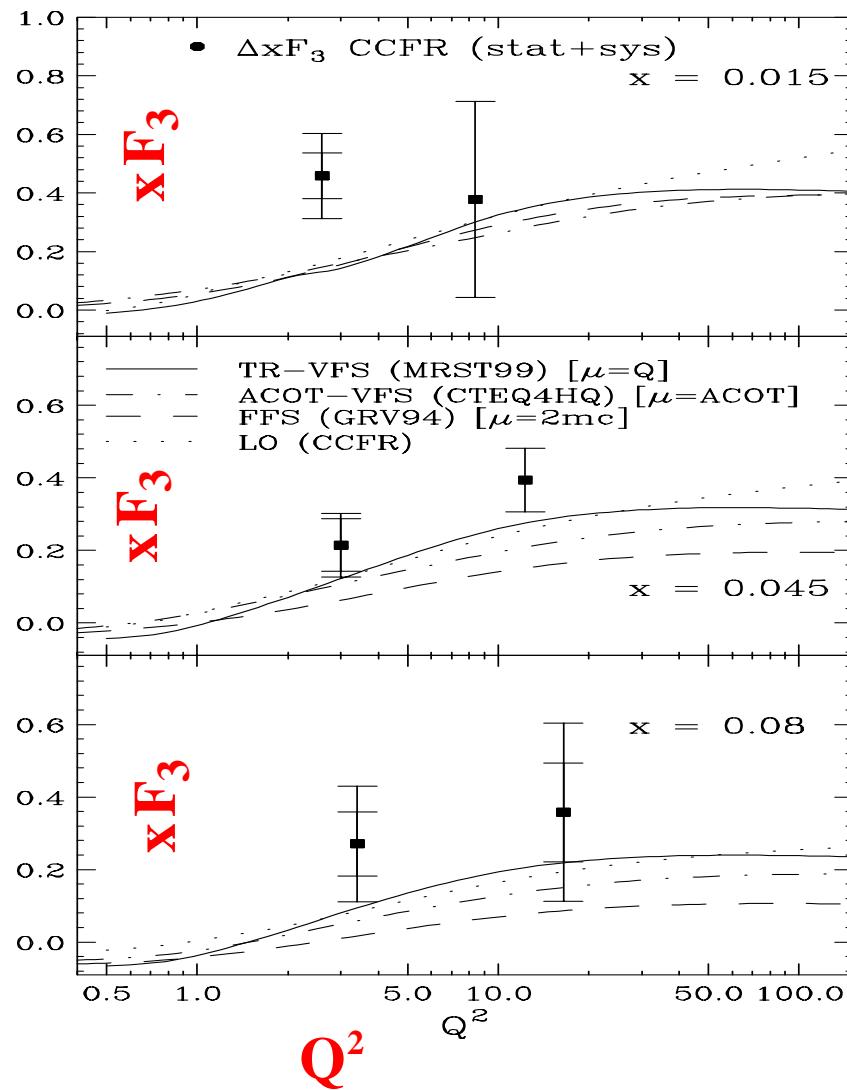
Three $\mu\mu$
events
observed



< 0.07 $\mu\mu$
event
expected

$N^0 \rightarrow \mu\mu\nu$???

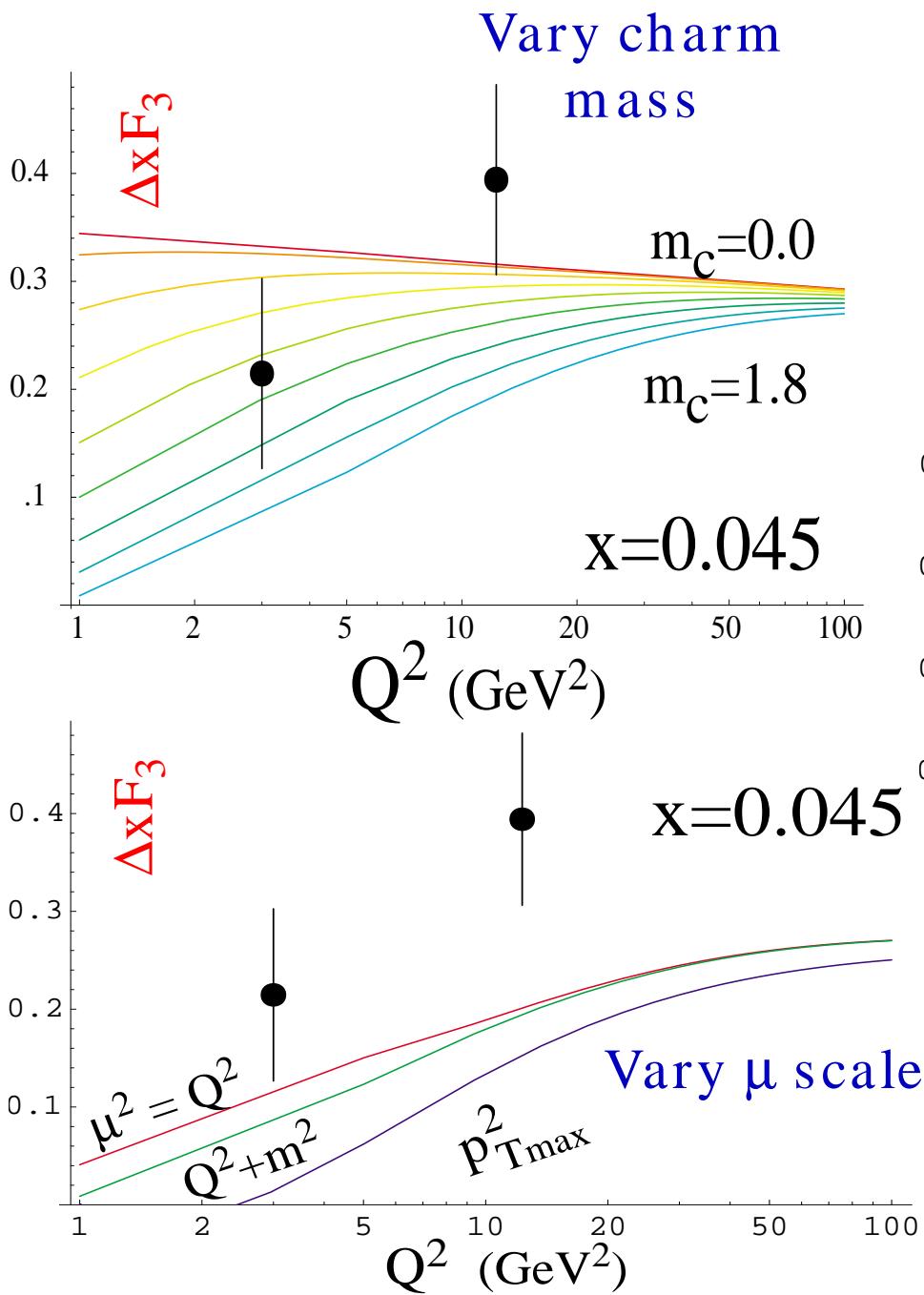
$\Delta x F_3$ Structure Function



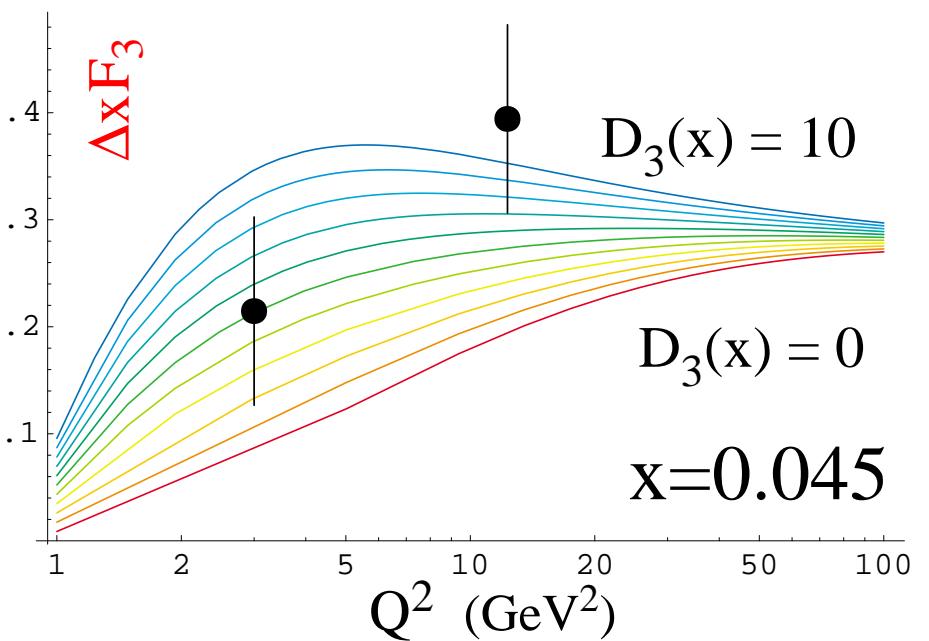
$$\Delta x F_3 \sim 4 x (s - c)$$

Un- Ki Yang
 NuTeV Collaboration
 PRL 86:2742 (2001)

Can we make the problem go away?



Vary higher twist contributions

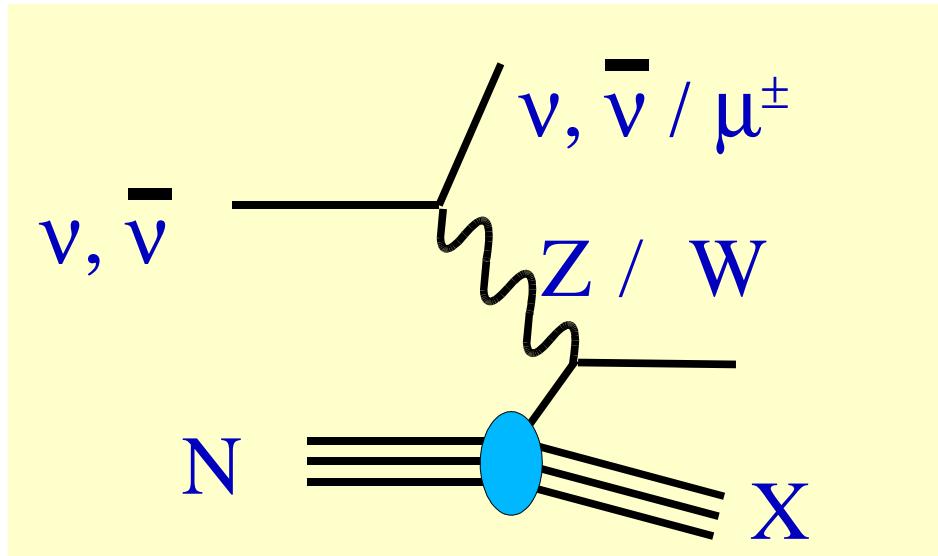


Question?

$$\Delta x F_3 \sim 4 x (s - c)$$

Could something
strange be
happening with the
heavy quarks?

Electroweak Mixing Angle Measurement



Paschos-Wolfenstein Relation:

$$R^- \equiv \frac{\sigma(\nu_\mu N \rightarrow \nu_\mu X) - \sigma(\bar{\nu}_\mu N \rightarrow \bar{\nu}_\mu X)}{\sigma(\nu_\mu N \rightarrow \mu^- X) - \sigma(\bar{\nu}_\mu N \rightarrow \mu^+ X)} \\ \approx \left(\frac{1}{2} - \sin^2 \theta_w \right)$$

NuTeV

Result: $\sin^2 \theta_W^{(on-shell)} = 0.2277 \pm 0.0031(stat) \pm 0.0009(syst)$

Standard Model Fit:

$\sin^2 \theta_W^{(on-shell)} = 0.2227 \pm 0.0004$ LEP EWWG

A 3σ difference

Contributions to Experimental Uncertainty

SOURCE OF UNCERTAINTY	$\delta \sin^2 \theta_W$	δR^ν	$\delta R^{\bar{\nu}}$
Data Statistics	0.00135	0.00069	0.00159
Monte Carlo Statistics	0.00010	0.00006	0.00010
TOTAL STATISTICS	0.00135	0.00069	0.00159
$\nu_e, \bar{\nu}_e$ Flux	0.00039	0.00025	0.00044
Energy Measurement	0.00018	0.00015	0.00024
Shower Length Model	0.00027	0.00021	0.00020
Counter Efficiency, Noise, Size	0.00023	0.00014	0.00006
Interaction Vertex	0.00030	0.00022	0.00017
TOTAL EXPERIMENTAL	0.00063	0.00044	0.00057
Charm Production, Strange Sea	0.00047	0.00089	0.00184
Charm Sea	0.00010	0.00005	0.00004
$\sigma^{\bar{\nu}}/\sigma^\nu$	0.00022	0.00007	0.00026
Radiative Corrections	0.00011	0.00005	0.00006
Non-Isoscalar Target	0.00005	0.00004	0.00004
Higher Twist	0.00014	0.00012	0.00013
R_L	0.00032	0.00045	0.00101
TOTAL MODEL	0.00064	0.00101	0.00212
TOTAL UNCERTAINTY	0.00162	0.00130	0.00272

TABLE I. Uncertainties for both the single parameter $\sin^2 \theta_W$ fit and for the comparison of R^ν and $R^{\bar{\nu}}$ with model predictions.

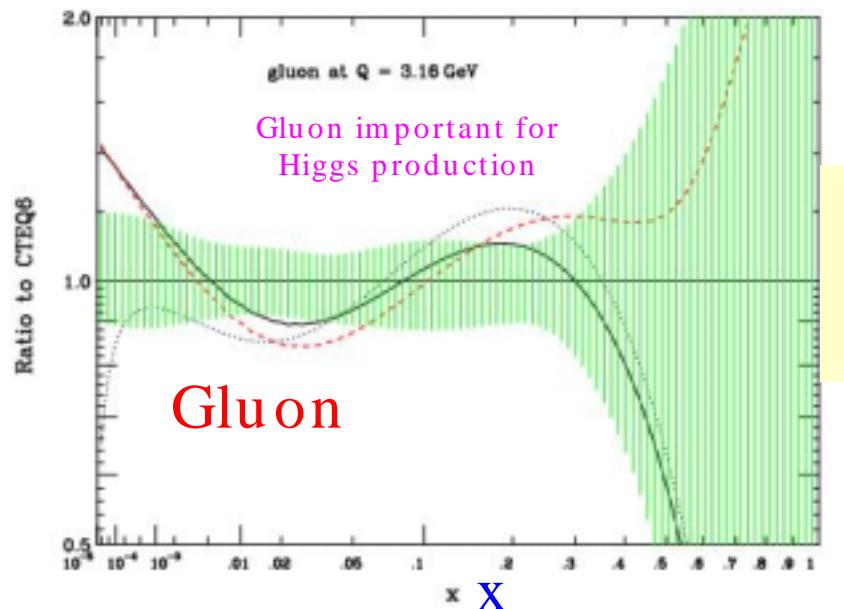
Largest model uncertainty arises from charm production and $s(x)$



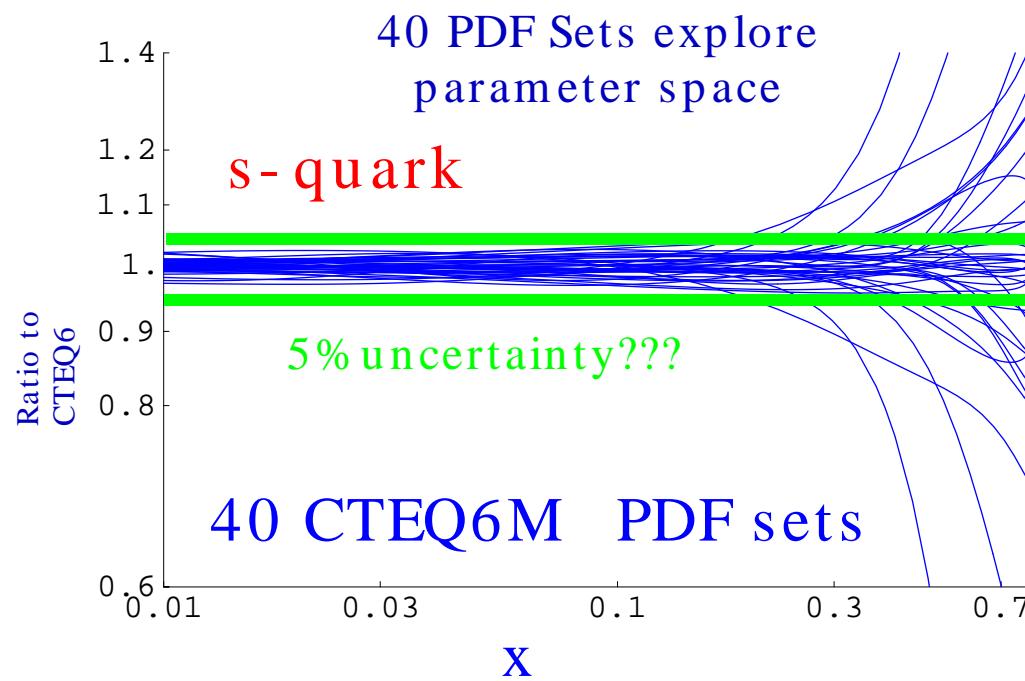
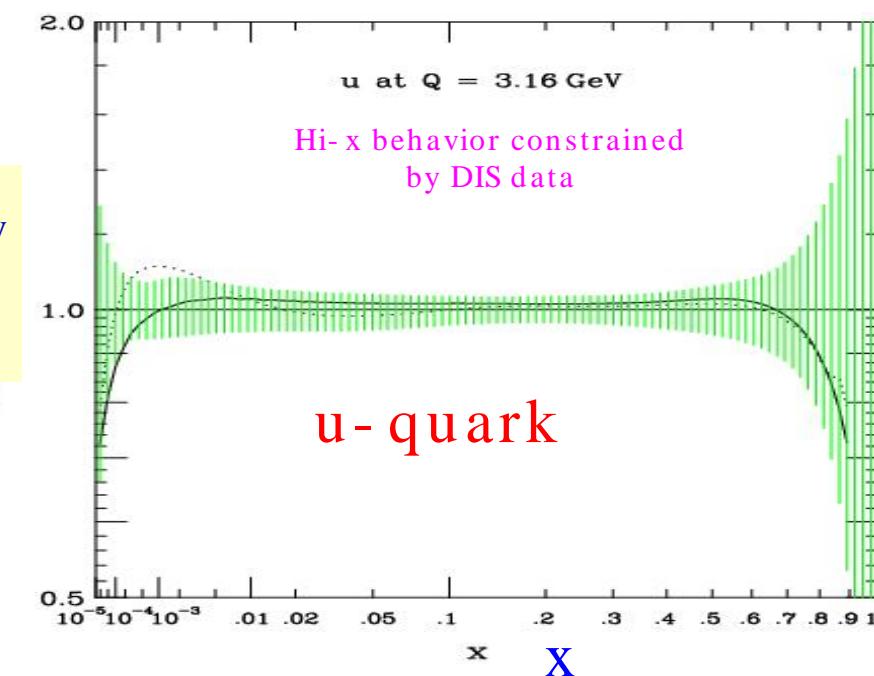
s and s -bar difference can have large effect

... relative uncertainty is reduced for combination

What is relative uncertainty on PDFs' ???



PDF Uncertainty
band compared
to CTEQ6M



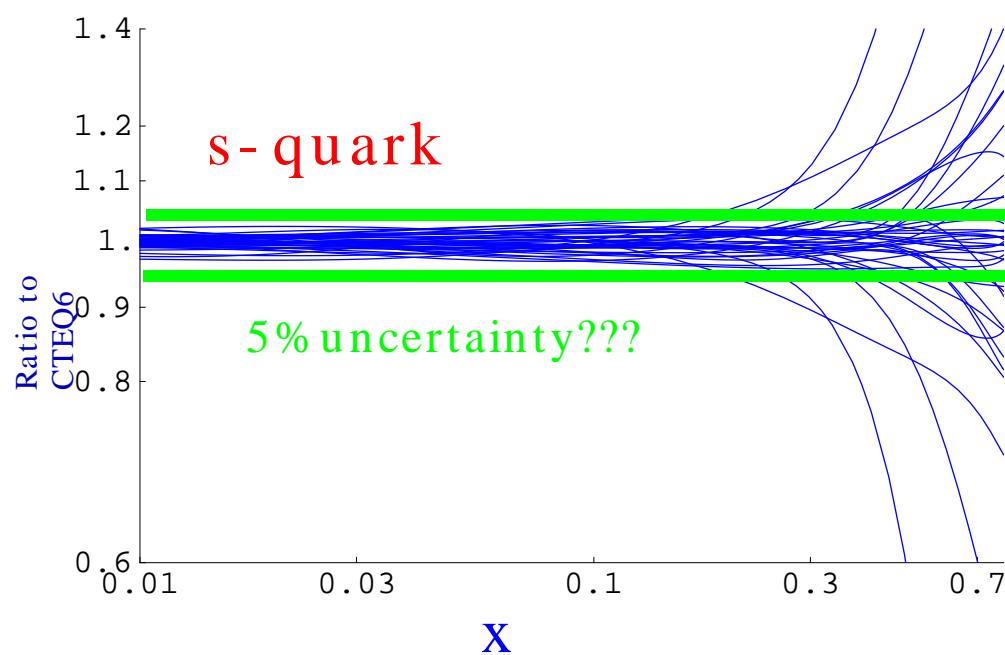
Previously, $s(x)$ was tied to u -bar and d -bar via kappa:

$$s(x) = \bar{s}(x) = \kappa \frac{\bar{u}(x) + \bar{d}(x)}{2}$$

Question: Do we really know the s-quark PDF to 5%???

What is true uncertainty on s-quark PDF???

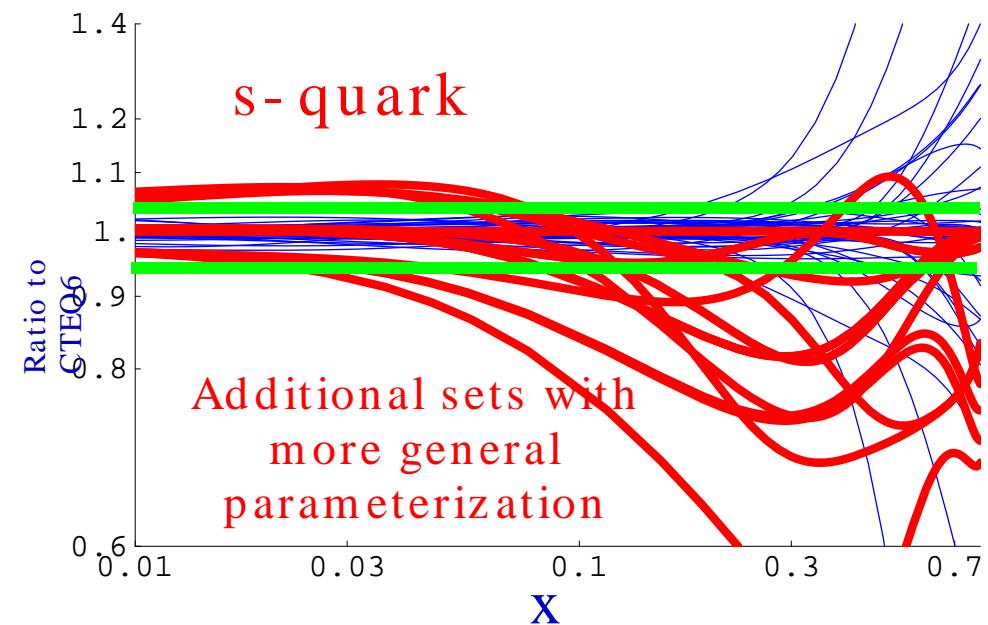
40 CTEQ6M PDF sets



s-quark

5% uncertainty???

Closer to the true error



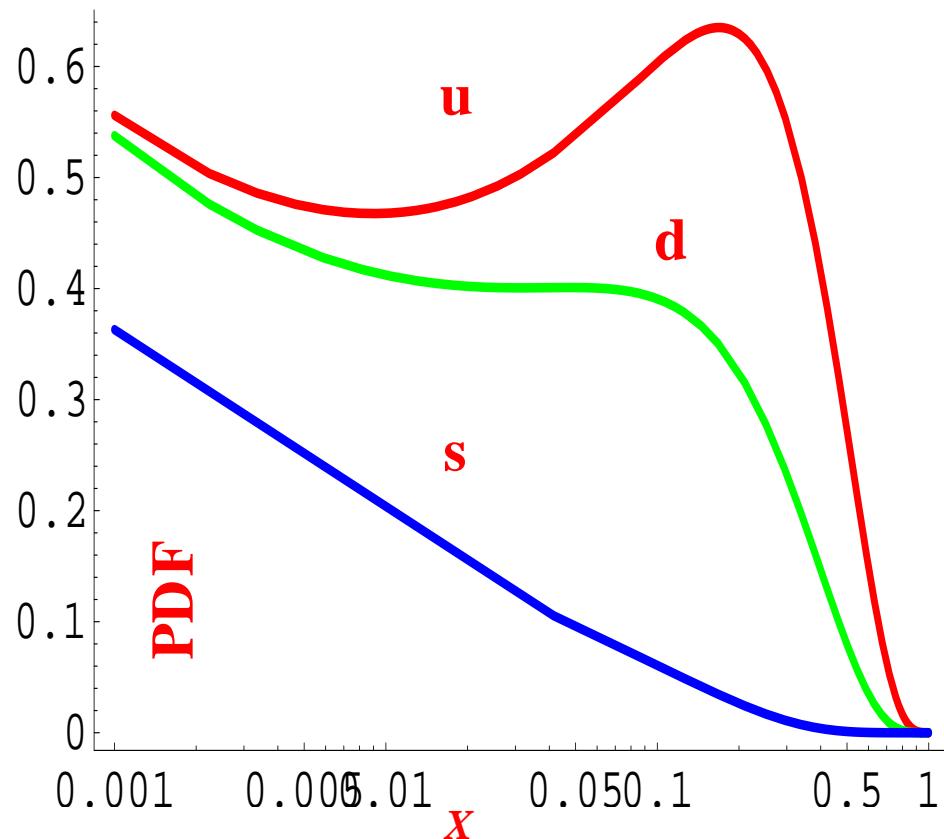
s-quark

Additional sets with
more general
parameterization

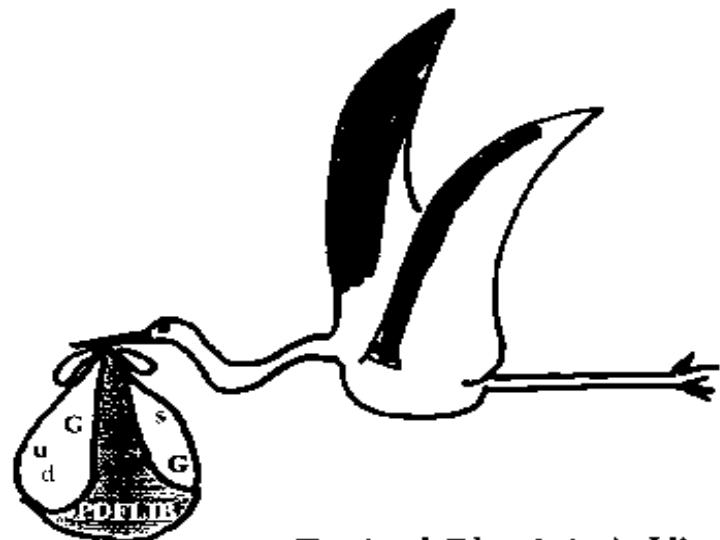
Curves shown are examples;
this is not an exhaustive set

Warning: The Director General has
determined the band of PDF's can
greatly underestimate the true
uncertainty

Where does $s(x)$ come from???



Where do PDF's come from???



Typical Physicist's View

Drawing by Heidi Schellman

Inclusive Structure Functions:

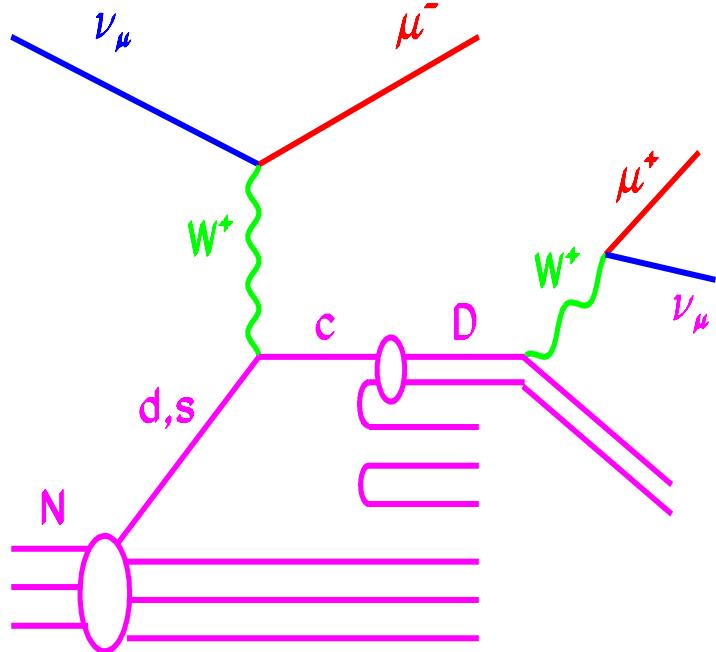
Yield $s(x)$ in combination

Must extract $s(x)$
from under other PDF's

$$F_2 \cong x (u + \bar{u} + d + \bar{d} + s + \bar{s} + c + \bar{c} + \dots)$$

... we can do better ...

Dimuons are ideal signal of $s(x)$



di- muon	NuTeV	CCFR	Combined
Neutrino	5012	5030	10042
Anti- Nu	1458	1060	2518

- * High stats & high precision data
- * Best constraints on strange quark

$$\frac{d \sigma_{\mu^\pm \mu^\mp}^+}{dx dy} = \int d\Gamma d\Omega \frac{d \sigma_{\mu^\mp c}}{dx dy d\Gamma} \otimes D_c(\Gamma) \otimes \Delta_c(\Omega)|_{E_{\mu^\pm} > 5 \text{ GeV}}$$

Di-muon
cross-section

Charm Production
cross-section

Fragmentation
Function

Decay
Distribution

Global Fit

χ^2 / DOF	CTEQ6M	Constrained	Mixed	Free
CCFR Nu	1.02	0.85	0.79	0.72
CCFR Nu-bar	0.58	0.54	0.59	0.59
NuTeV Nu	1.81	1.70	1.55	1.44
NuTeV Nu-bar	1.48	1.30	1.15	1.13
BCDMS F2p	1.11	1.11	1.11	1.11
BCDMS F2d	1.10	1.10	1.10	1.11
H1 96/97	0.94	0.95	0.94	0.94
H1 98/99	1.02	1.03	1.03	1.03
ZEUS 96/97	1.14	1.14	1.14	1.15
NMC F2p	1.52	1.50	1.51	1.49
NMC F2d/ F2p	0.91	0.91	0.91	0.91
MC F2d/ F2p < Q^2 >	1.05	1.07	1.06	1.03
CCFR F2	1.70	1.71	1.81	1.88
CCFR F3	0.42	0.42	0.44	0.42
E605	0.82	0.82	0.82	0.83
NA51	0.62	0.61	0.52	0.52
CDF ℓ Asym	0.82	0.83	0.82	0.82
E866	0.39	0.40	0.39	0.38
D0 Jets	0.71	0.65	0.70	0.67
CDF Jets	1.48	1.48	1.48	1.47
TOTAL	2173	2144	2142	2133

Total of 1991 data points

Reasonable χ^2 values
(CTEQ6 did not fit di-muon data)

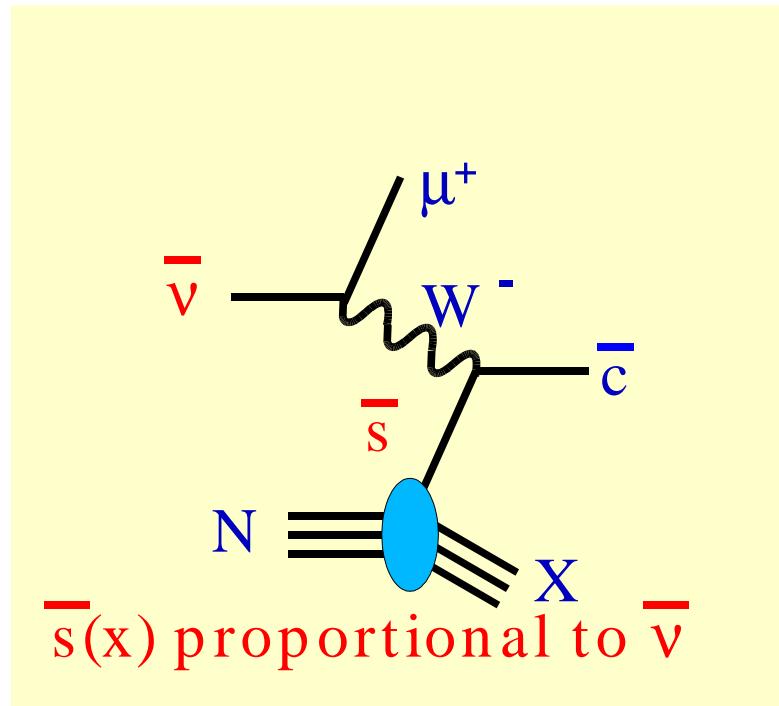
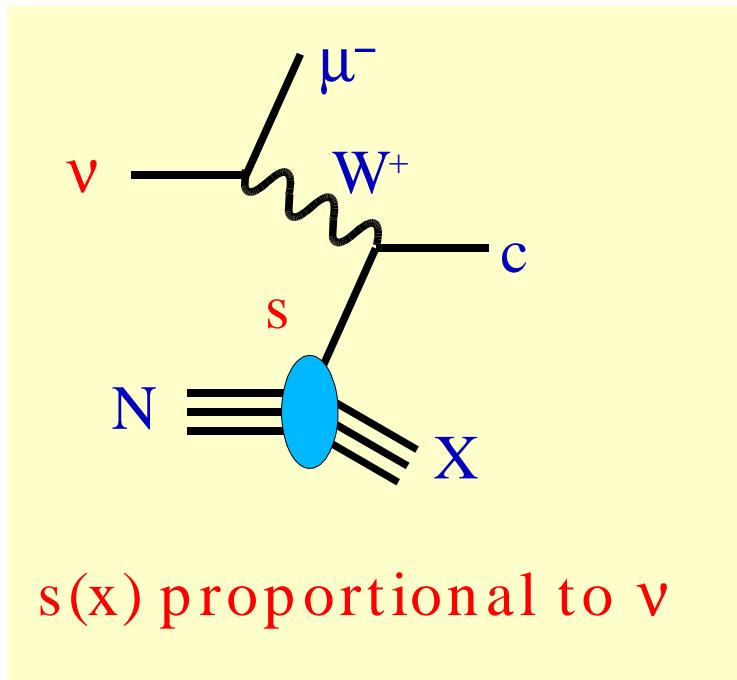
More parameters,
lower value of χ^2

Only di-muon data is
sensitive to $s(x)$!!!

⋮

Idea: v and v -bar data
separately determine
 s and s -bar
distributions

Sign-selected beam separates ν and $\bar{\nu}$: Extract s and \bar{s}

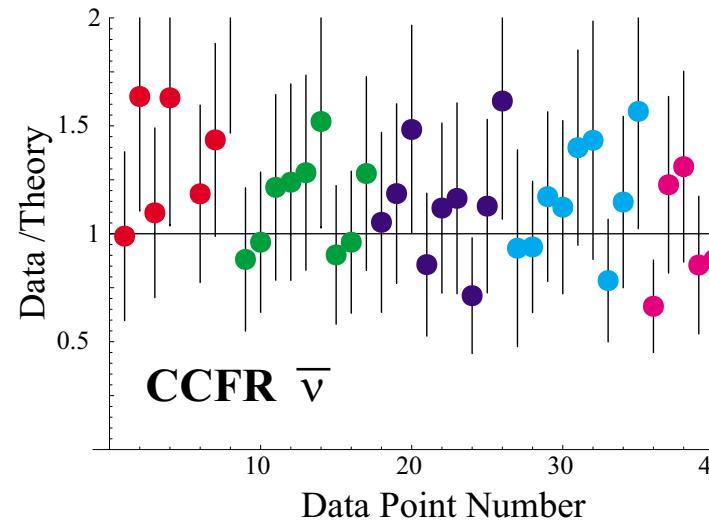
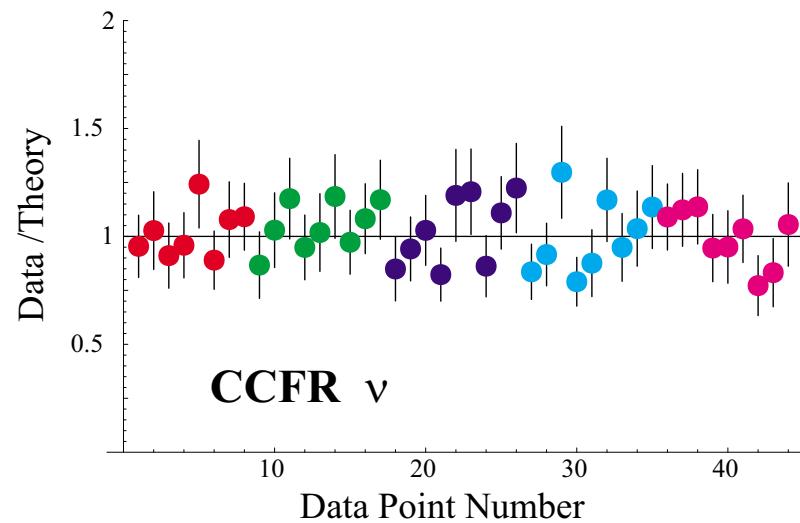


* Other data sets are insensitive to $s(x)$

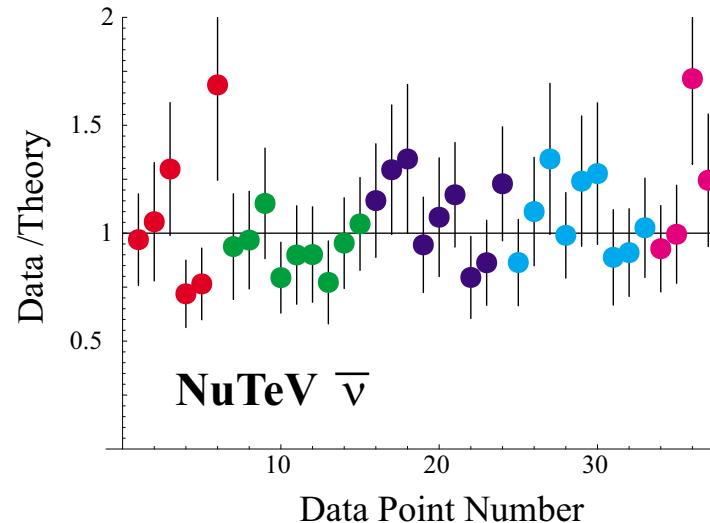
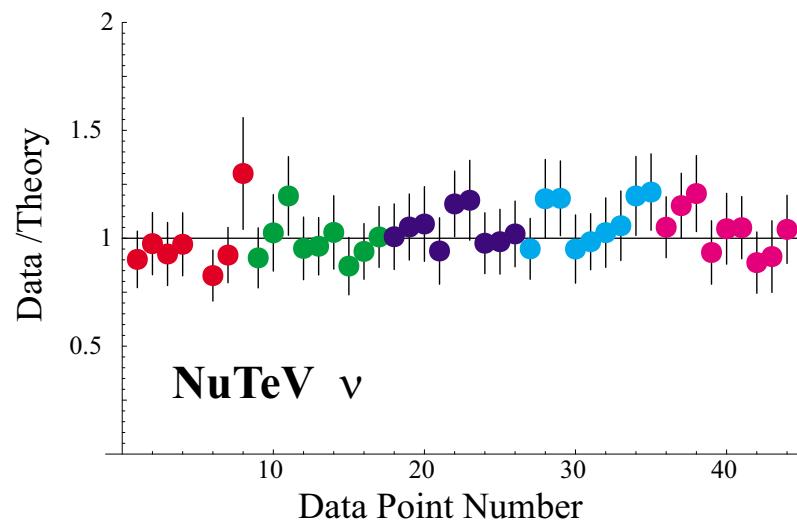
* Caution: ensure quark number sum rule is satisfied

$$\int dx [s(x) - \bar{s}(x)] = 0$$

How good is the fit? (Data - Theory)/ Theory Plots

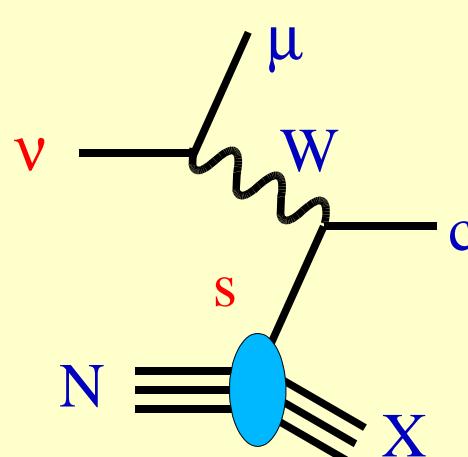


PRELIMINARY



Higher statistics for ν - data \Rightarrow stronger pull for fit

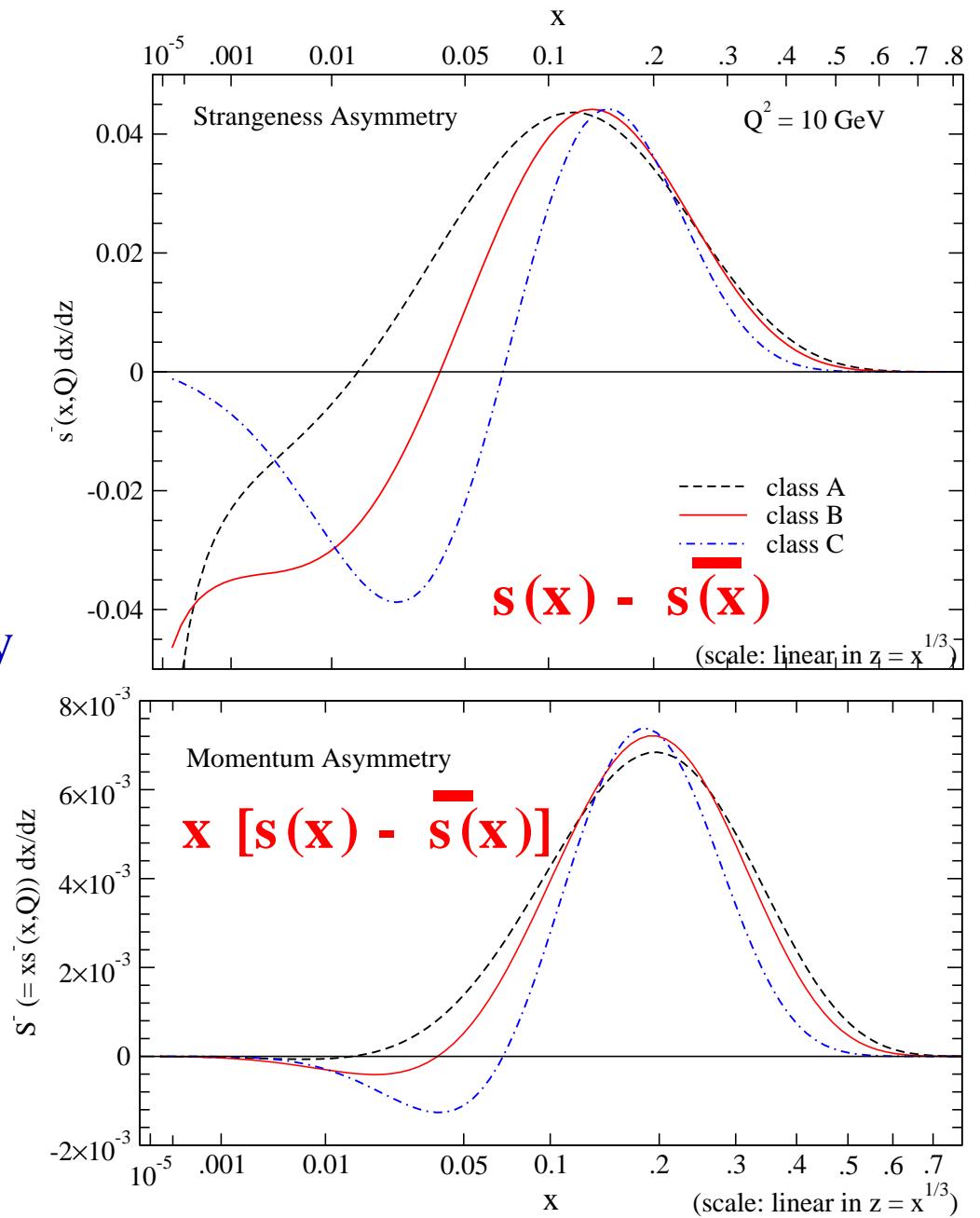
What does the strange PDF look like?



General range of the asymmetry

$$[S^-] \equiv \int_0^1 x \{ s(x) - \bar{s}(x) \}$$

$$+0.40 \geq 100 \times [S^-] \geq -0.10$$



What is the range of the $s - \bar{s}$ Asymmetry?

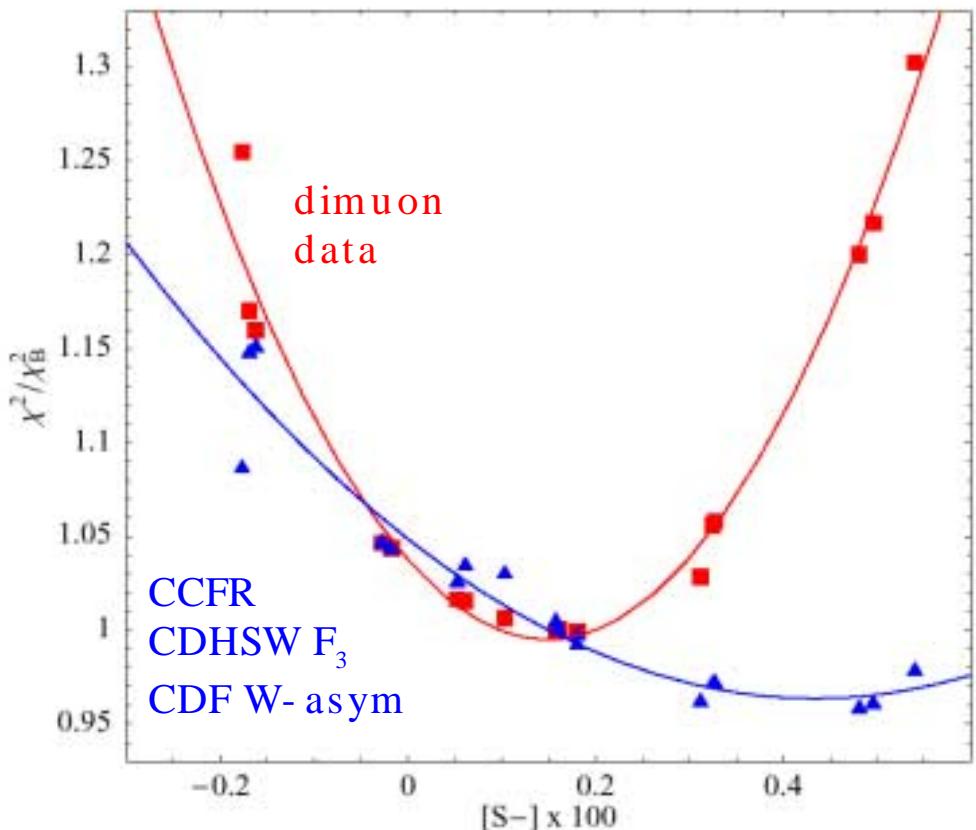
General range of the asymmetry

$$[S^-] \equiv \int_0^1 x \{ s(x) - \bar{s}(x) \}$$

$$+0.40 \geq 100 \times [S^-] \geq -0.10$$

$s - \bar{s}$: large uncertainty affected by:

- charm fragmentation
- charm mass
- PDF set



	# pts	B+	A	B	C	B-
$A_1 + b$	-	-0.78	-0.99	-0.78	0	-0.78
$[S^-] \times 100$	-	0.540	0.312	0.160	0.103	-0.177
Dimuon	174	1.30	1.02	<i>1.00</i> (126)	1.01	1.26
Inclusive I	194	0.98	0.97	<i>1.00</i> (141)	1.03	1.09
Inclusive II	2097	1.00	1.00	<i>1.00</i> (2349)	1.00	1.00

{

 CCFR

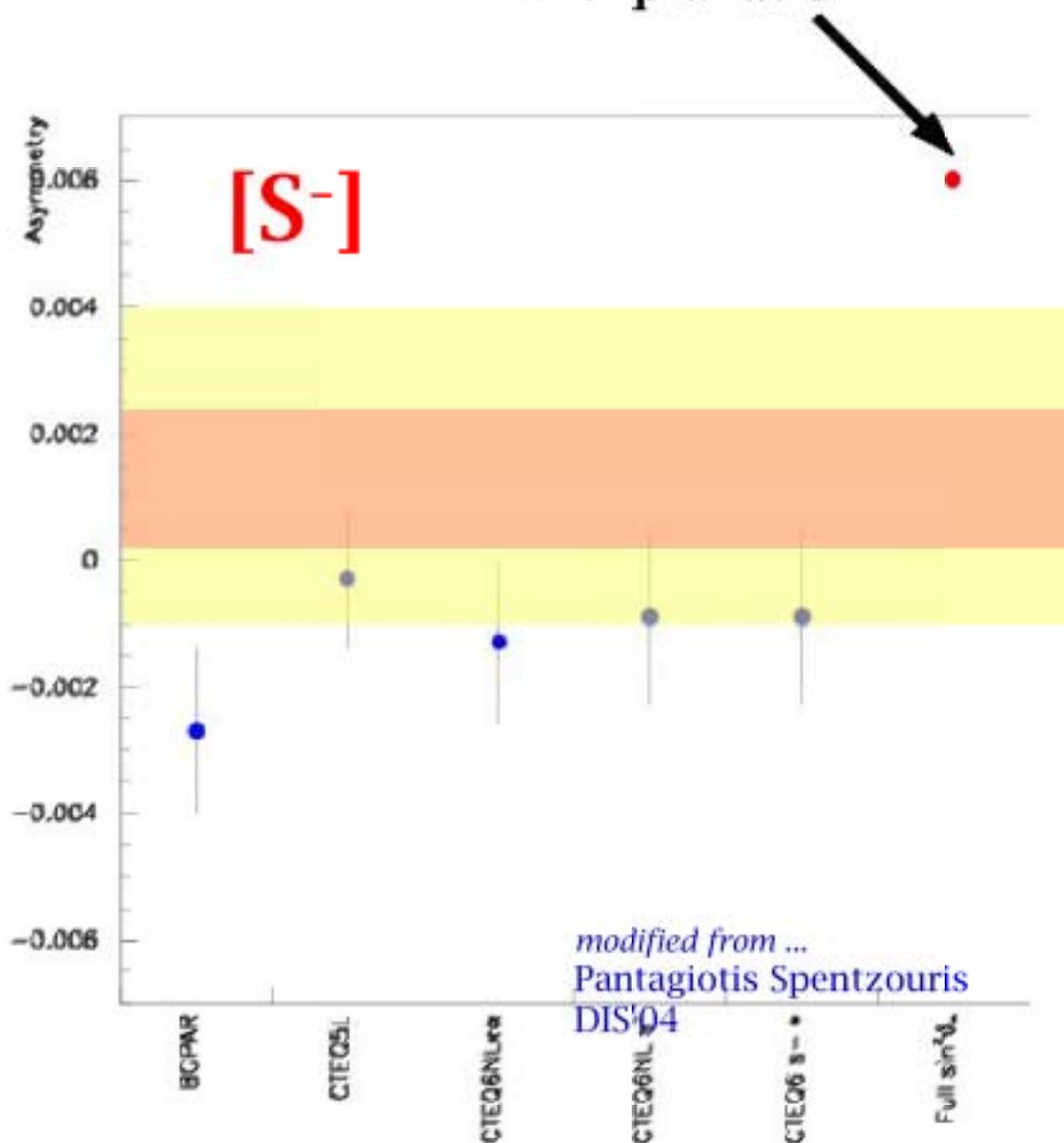
 CDHSW F₃

 CDF W- asym

What is the status:

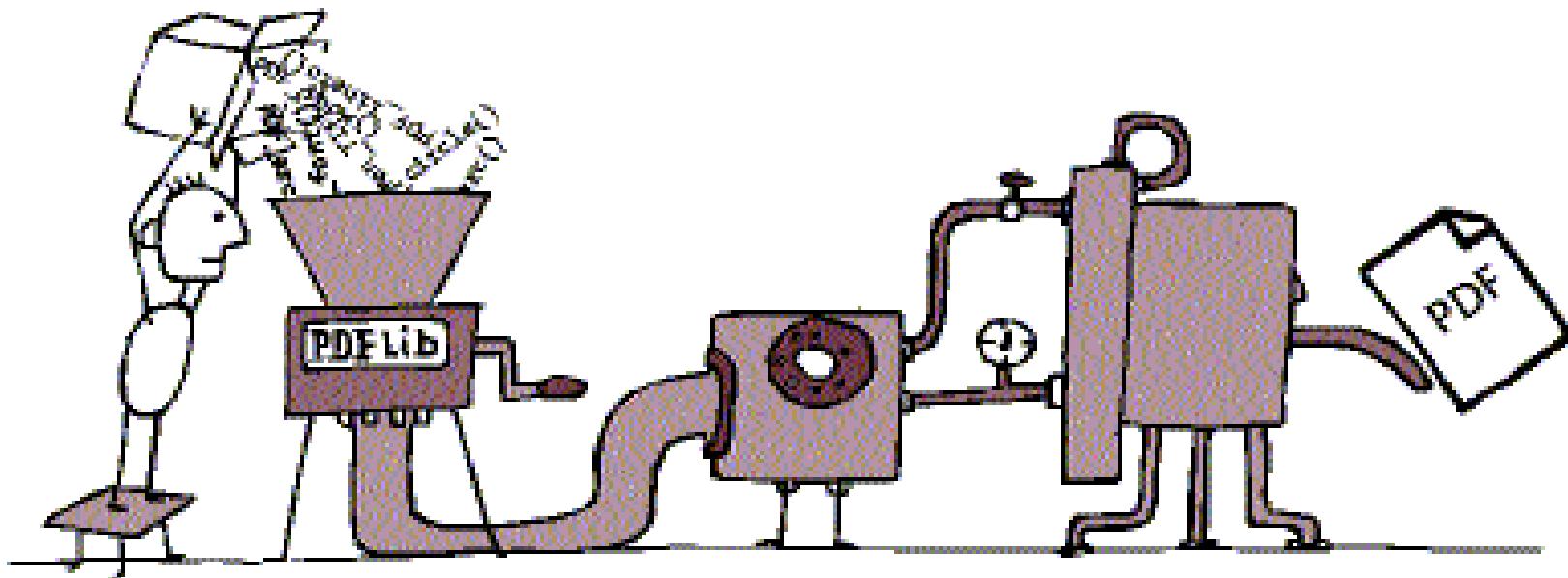
- Tremendous new information on $\bar{s}+s$
- $s-\bar{s}$: large uncertainty affected by:
 - charm fragmentation
 - charm mass
 - PDF set
- Strong interplay between the existing experimental constraints and the global theoretical constraints, particularly the # sum

level needed for EW explanation



That was LO

How do we make
heavy quarks at NLO???



A Thought Experiment:

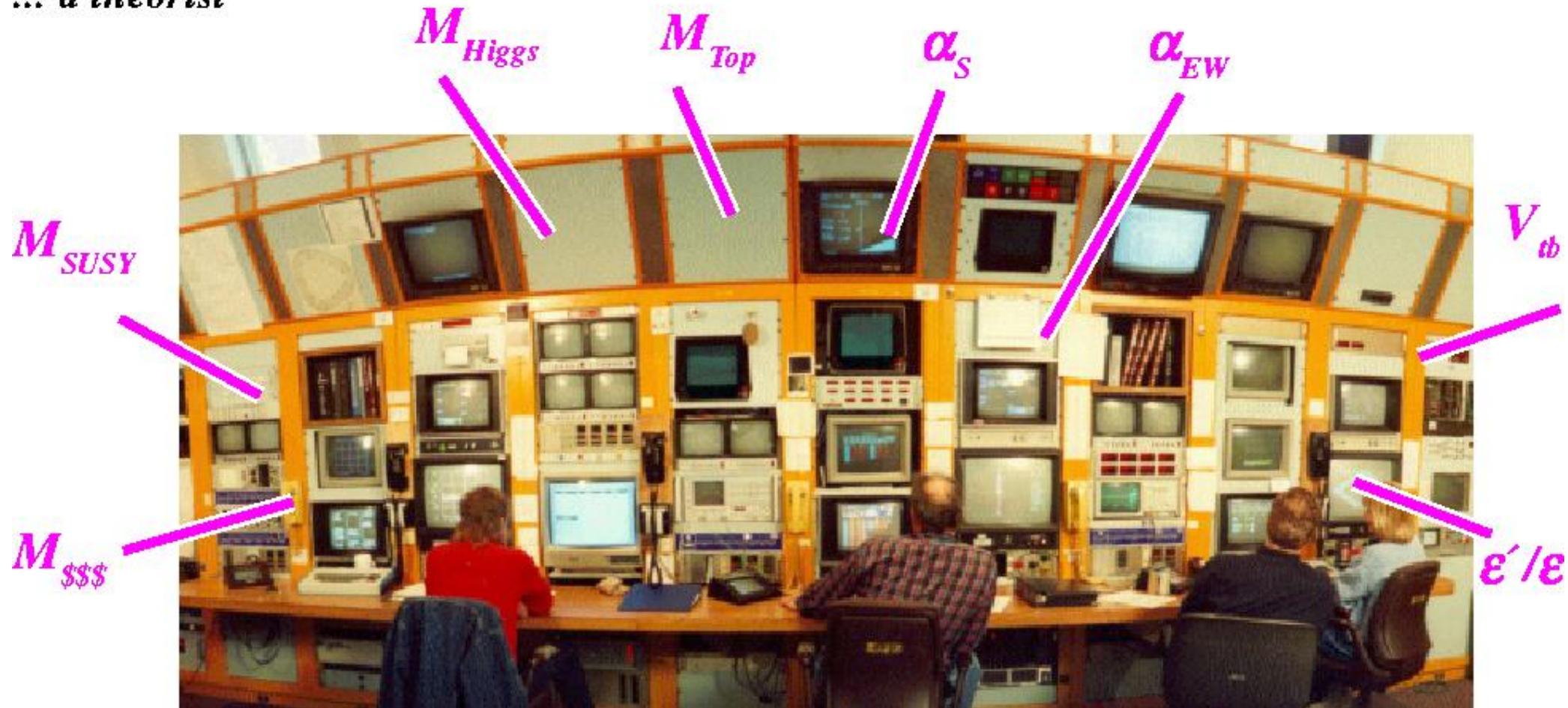
What is the ideal way to learn about quark masses and their effects on a physical process?

As a theorists, I simply run my calculation over the full range of mass values from 0 to ∞ , and study the behavior.

Wouldn't it be great if the experiments could do the same???

What's really in the Experimental control room ...

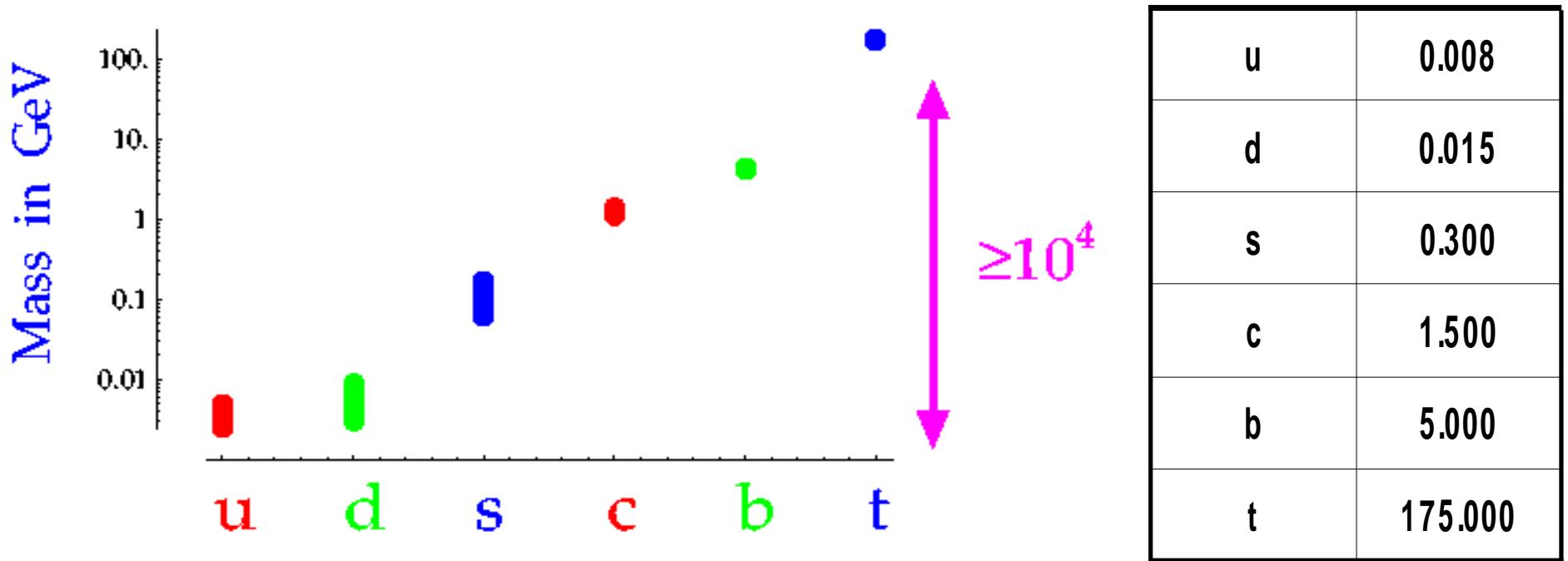
... a theorist



Unfortunately, in real life, we can't vary parameters continuously

The UP Side

Quark Masses Span Wide Dynamical Range $\sim 10^4$



We can't vary the quark mass continuously, but these ``notches'' on our control panel give us a lot of flexibility

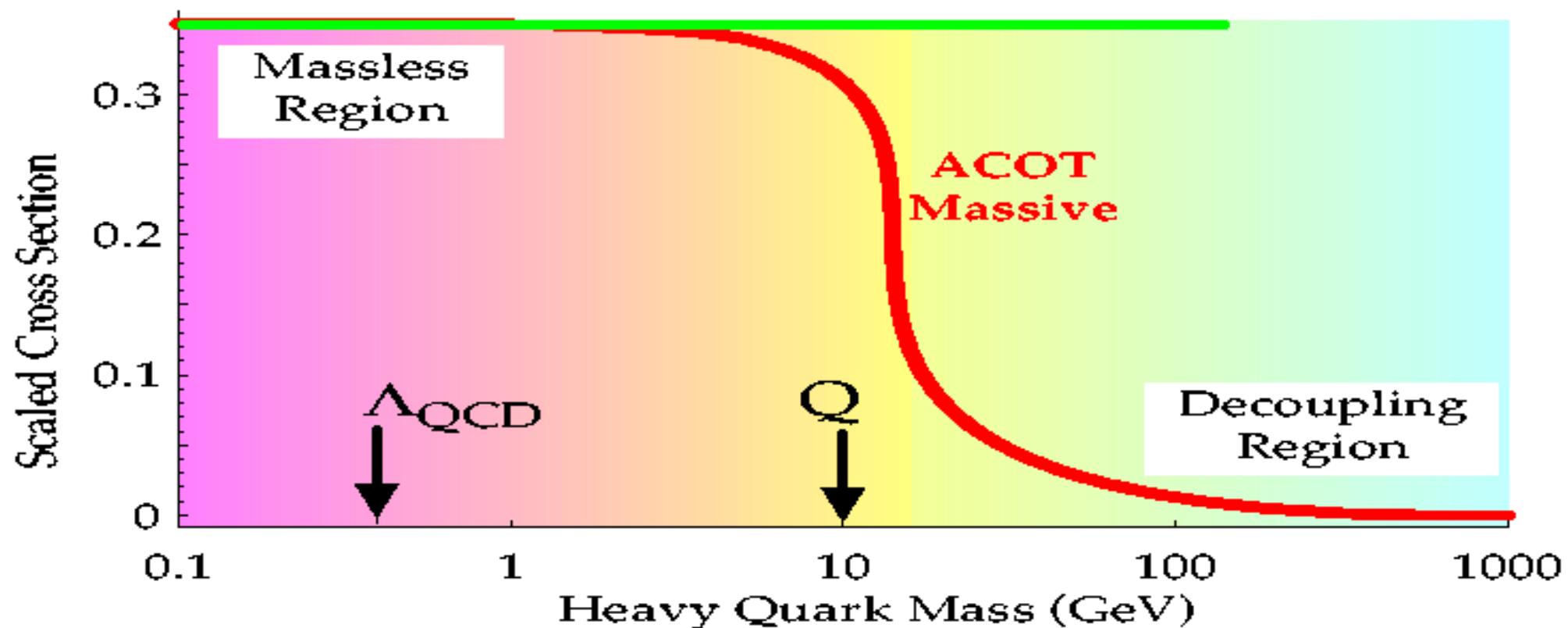
The DOWN Side

Theorists would much prefer that quark masses only come in 2 varieties:

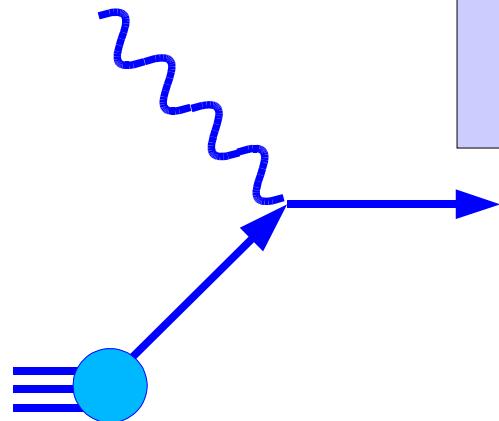
$m = 0$: Massless case.
Mass plays no dynamic role
Well understood.

$m = \infty$: Infinite case.
Mass Decouples.
We can forget about this object

MS-Bar Massless



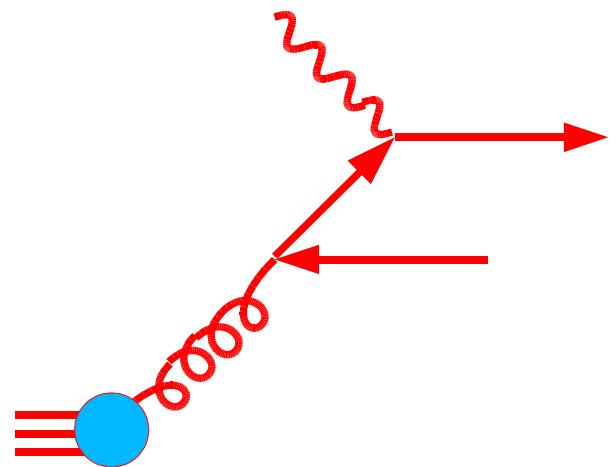
Production of Heavy Quarks: The Problem



Heavy Excitation (HE)

Quark	Channel
s	YES
t	NO
c	???
b	???

Which is the correct production mechanism?

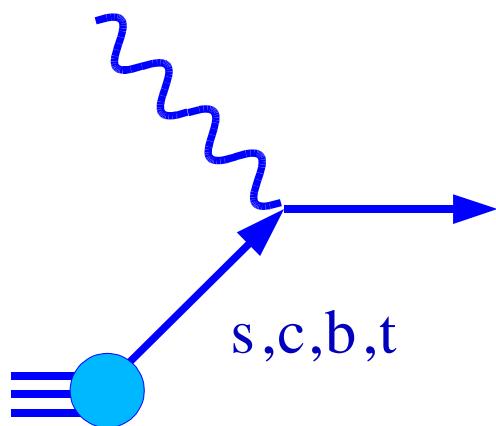


Heavy Creation (HC)

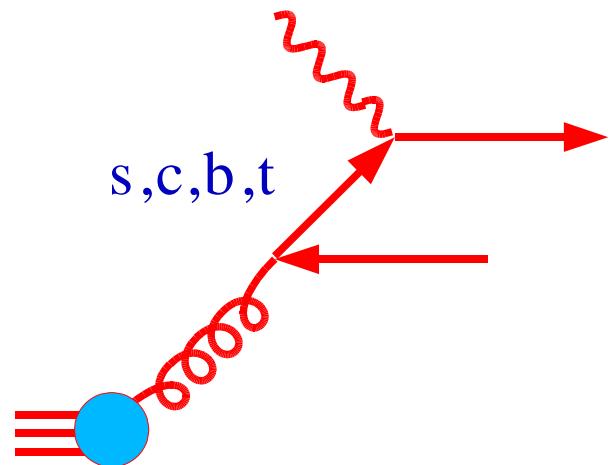
Quark	Channel
s	NO
t	YES
c	???
b	???

If you can't beat 'em, join 'em.

How to Join without ``Double Counting"???

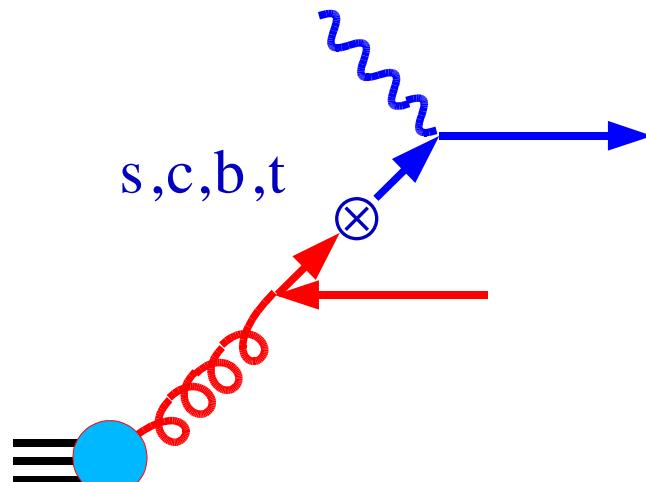


Heavy Excitation (HE)

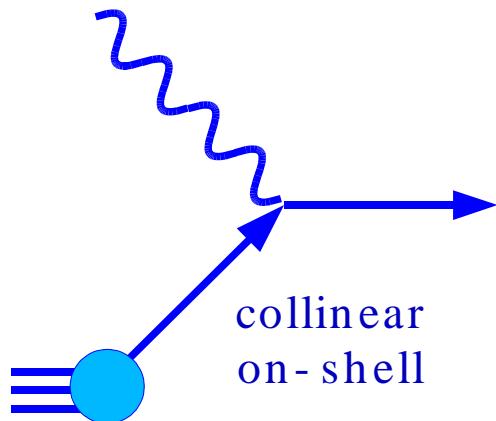


Heavy Creation (HC)

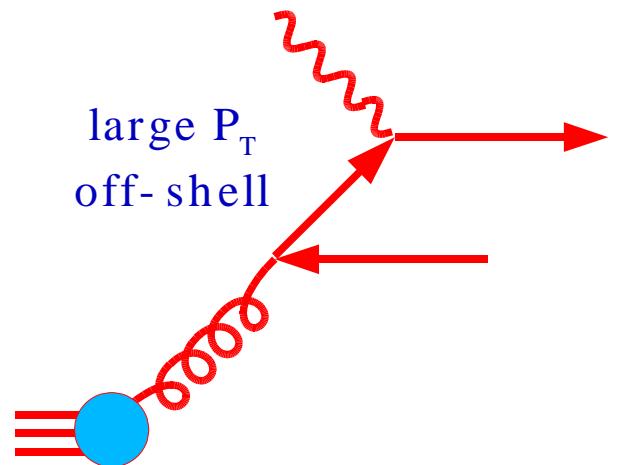
Wait a minute!
Since the heavy
quark originally
came from a gluon
splitting, these
diagrams are
Double Counting



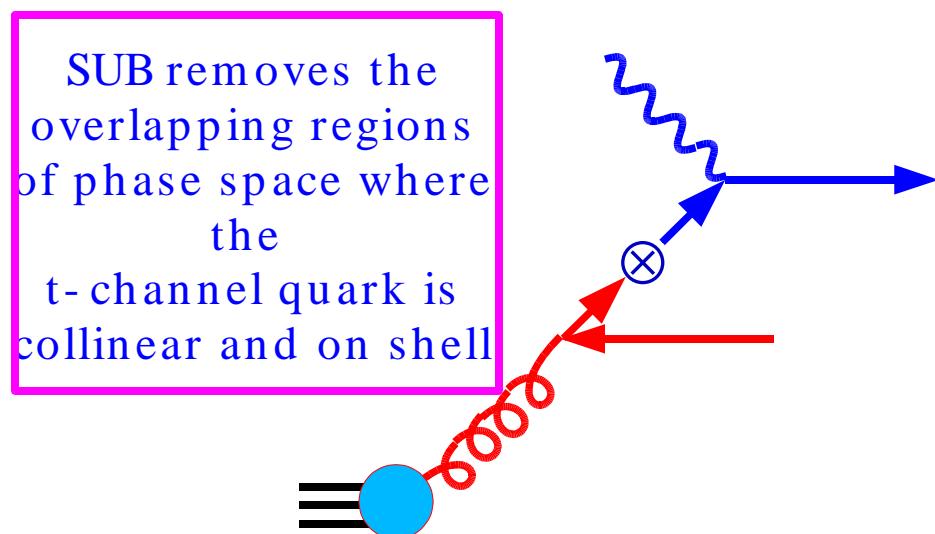
How to Join without ``Double Counting"???



Heavy Excitation (HE)



Heavy Creation (HC)



Subtraction (SUB)

$$TOT = HE + \underbrace{(HC - SUB)}$$

Formally, NLO

There is a rigorous factorization proof ...

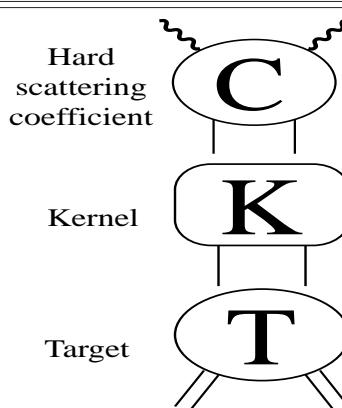
A formal proof
was constructed
by numerous
groups.

Ingredients of Factorization

Decompose into (t-channel) 2PI amplitudes:

$$\sigma = \sum_{N=1}^{\infty} C(K)^N T + \text{Non-leading}$$

Collins, Soper, Sterman. Perturbative QCD, World Scientific (1989). Collins, in preparation



After reorganization of the infinite sum:

Parton Model	Remainder
$\overbrace{C [1 - (1-Z) K]^{-1} Z [1 - K]^{-1} T}^{\substack{\text{Wilson Coefficient} \\ (\text{Hard Scatt. } \hat{\sigma})}}$	$\overbrace{C [1 - (1-Z) K]^{-1} (1-Z) T}^{\substack{\text{Parton} \\ \text{Distribution} \\ \text{Power} \\ \text{Suppressed}}}$
Z: collinear projection	

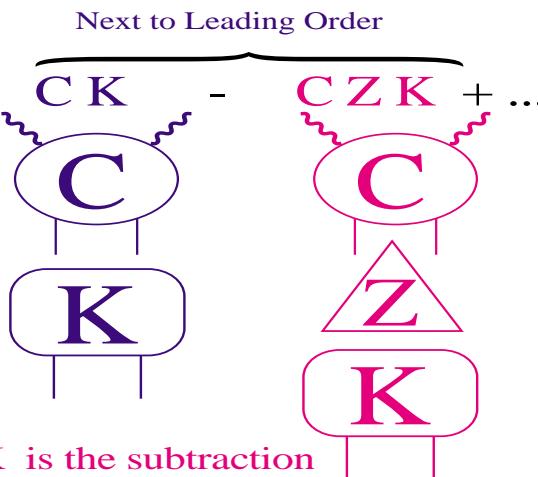
Wilson Coefficient:

$$C [1 - (1-Z) K]^{-1} \approx$$

All orders result



Wilson Coefficient:
IR safe “hard”
scattering cross section



C Z K is the subtraction

This proof was
explicitly extended
to the case of
massive quarks

(Collins, 1998)

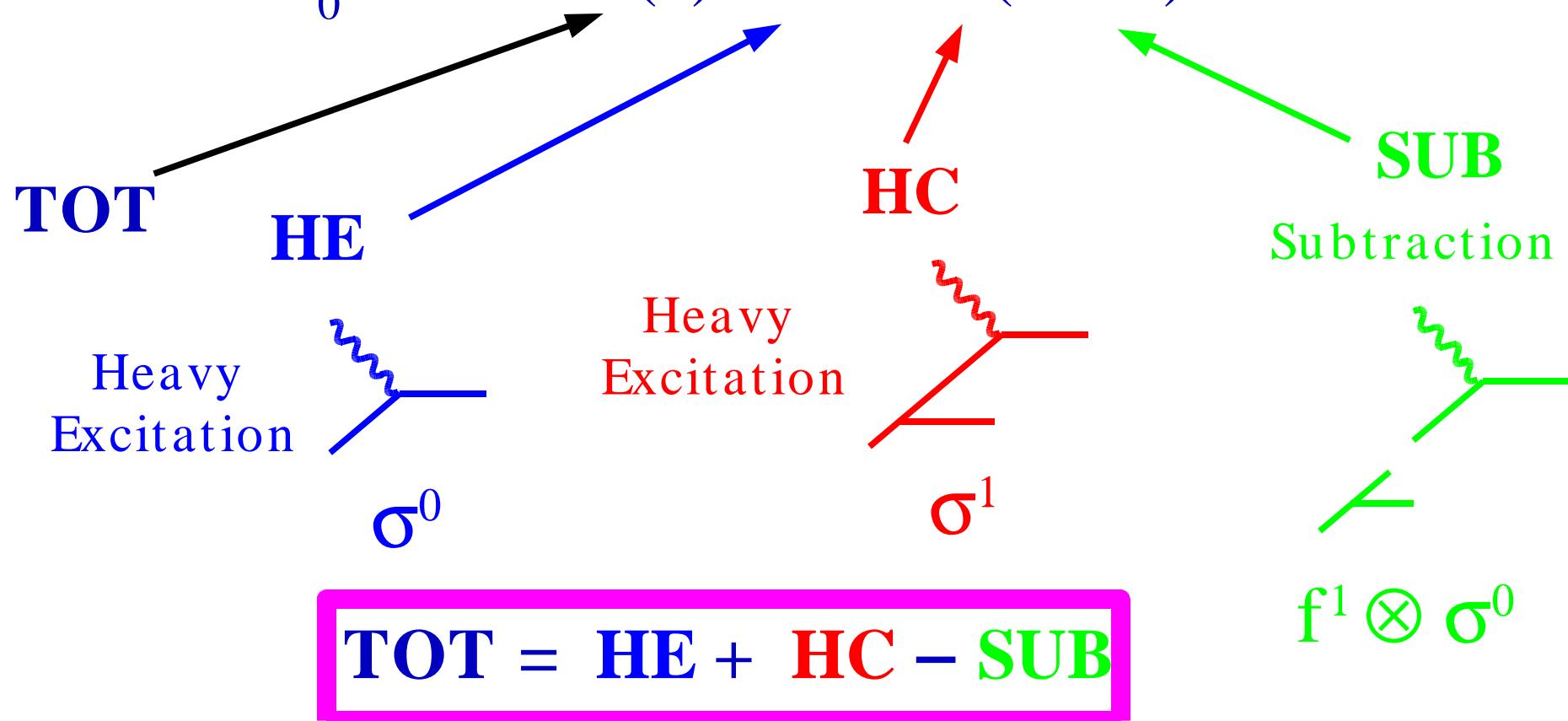
THOUGH
EXPERIMENT
To keep things
simple, let's
consider
scattering
off a parton target.

An Example: How the separate pieces can conspire

Expand $f(x) = x$ in Taylor Series about x_0 .

For $x_0 = 0$: $f(\varepsilon) = 0 + (\varepsilon - 0) + \dots = \varepsilon$

For $x_0 = 1$: $f(\varepsilon) = 1 + (\varepsilon - 1) + \dots = \varepsilon$



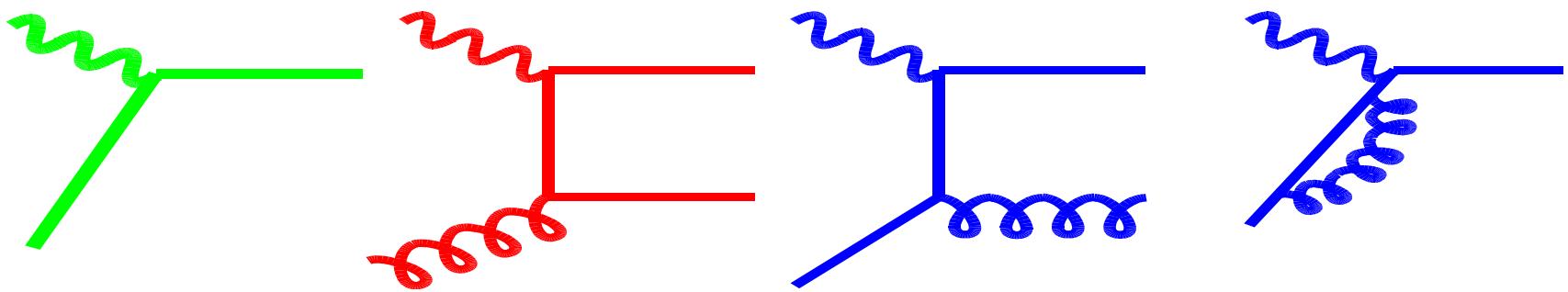
The Moral

**It doesn't matter which expansion point you use;
QCD will compensate (if you go to high enough order).**

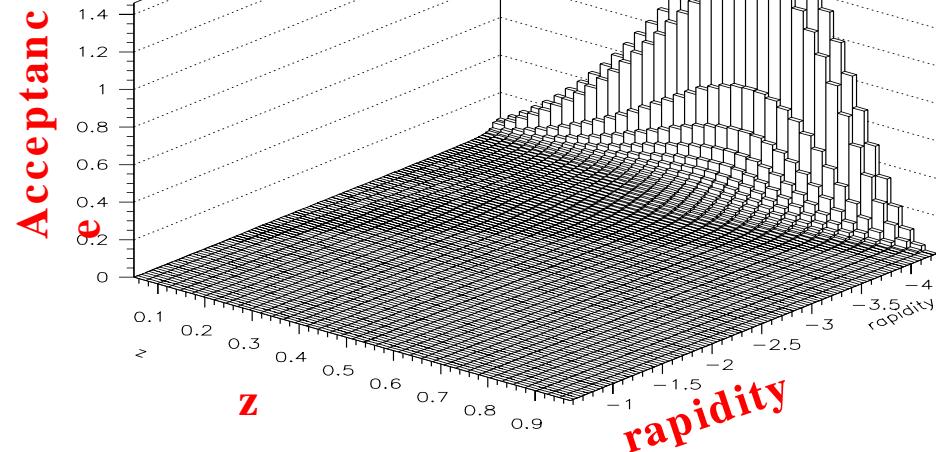
In practice ...

**we are often limited to low-order calculations,
so it is wise to choose your expansion point carefully.**

NLO Analysis: In progress ...

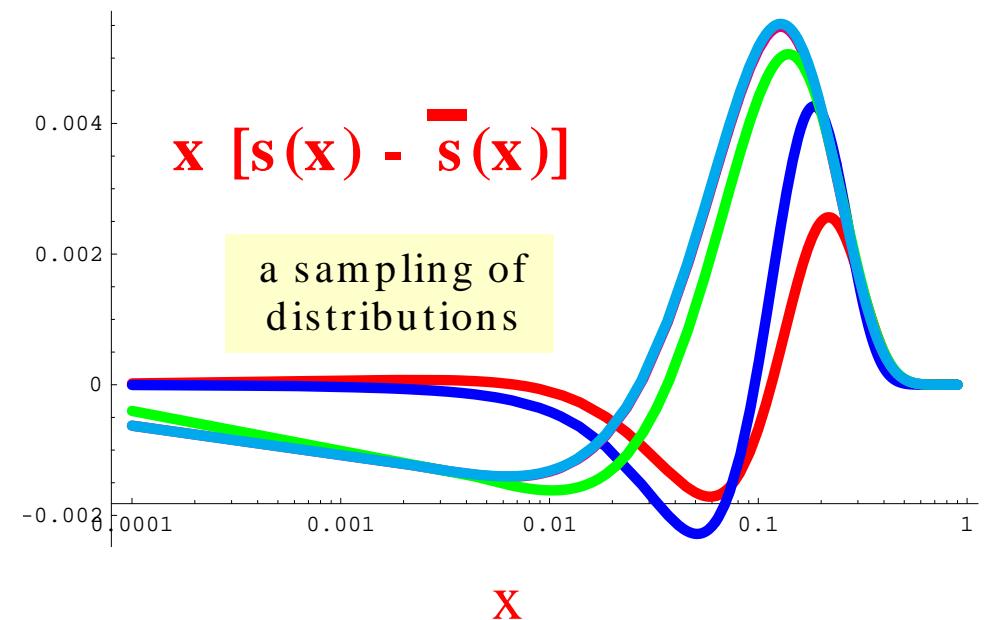


DISCO numerical Fortran program
available for data analysis



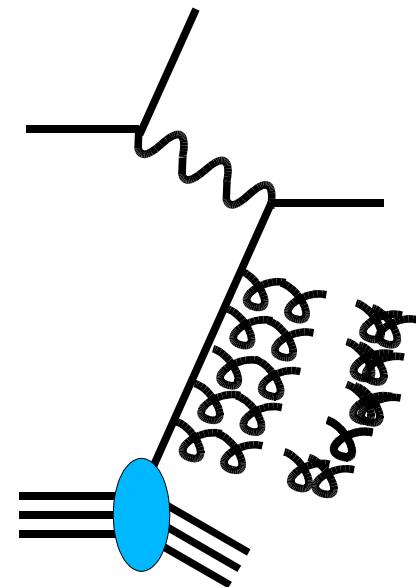
Kretzer, Mason, Olness PRD 65:074010 (2002)

- * Higher order diagrams
- * More differential distributions
- * Encounter : $\delta(p_T)$ and $1/(1-x)_+$



Future Work: Resummation of soft gluons for massive processes

- * Uses CSS Formalism to resum $\log(q_T/Q)$
- * Uses ACOT Formalism to resum $\log(M/Q)$



Satisfies appropriate limits:

$q_T \rightarrow Q$, obtain usual perturbative result

$M \rightarrow 0$, obtain usual massless result

$M, q_T \rightarrow 0$, obtain usual Sudakov form

Theoretical basis for NLO Monte Carlo program
... provides full kinematic description

Summary

- * Di-Muon data incorporated in Global fit:

- Provides important information on $s(x)$

- Important for search for "New Physics" signals

- * NLO Experimental Dimuon analysis:

- NLO Experimental analysis in progress (D. Mason)

- NLO code (DISCO) is available (S. Kretzer)

- * Need to consider $s \neq s\text{-bar}$

- This is real progress!!! We now can discriminate!

- Large uncertainties; must fully characterize effects;
include NLO

- Analysis in progress

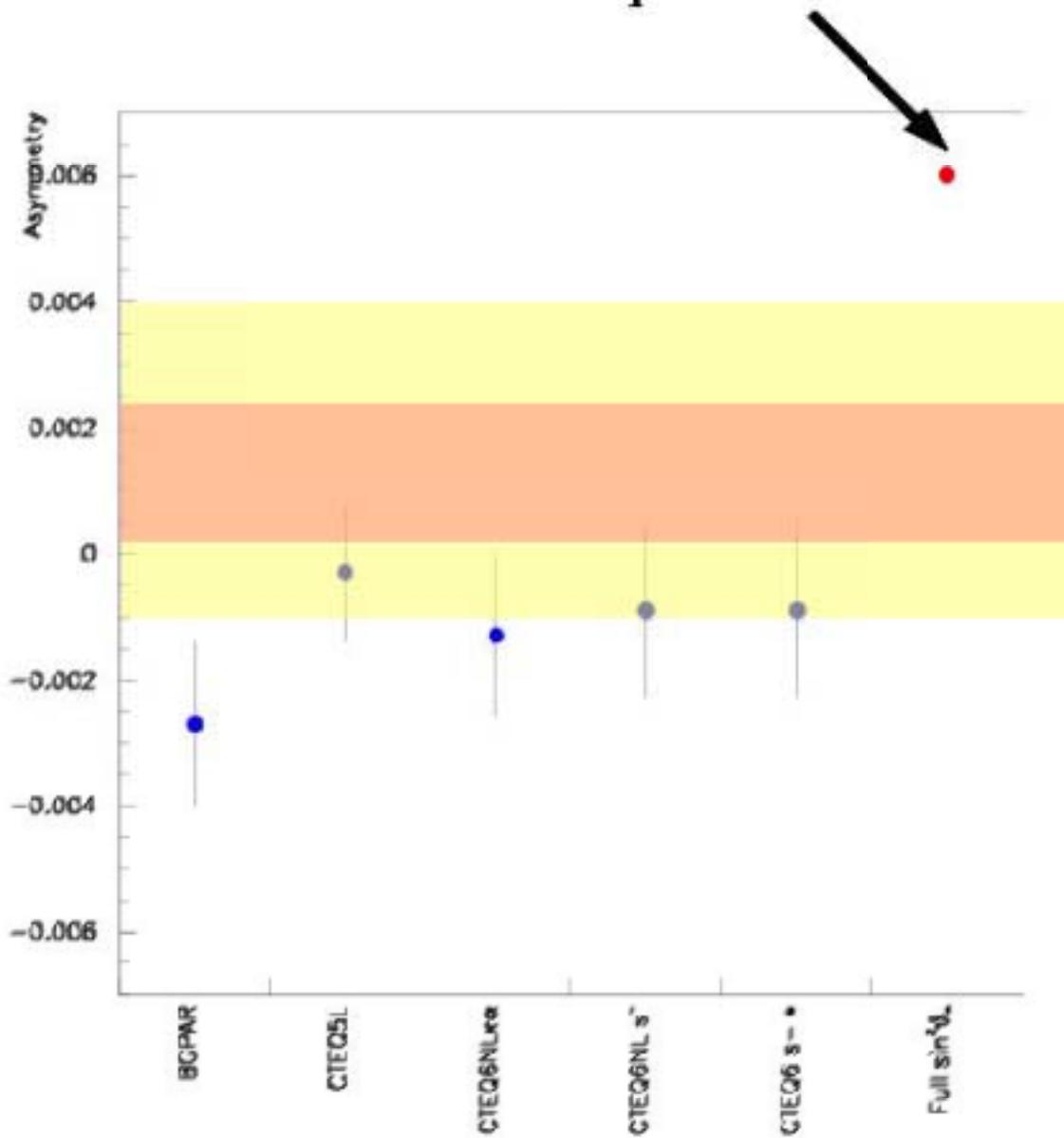
- * Resummation of large logarithms:

- Resummation of $\log(q_T/Q)$ and $\log(M/Q)$ (P. Nadolsky ...)

What is the status:

- Tremendous new information on s + s
- s - s: large uncertainty affected by:
 - charm fragmentation
 - charm mass
 - PDF set
- Strong interplay between the existing experimental constraints and the global theoretical constraints, particularly the # sum rule

level needed for EW explanation



Conclusions

- * Many outstanding puzzles, even with data already on tape:
 - Higher Twist
 - Up and Down PDF's at large x
 - Nuclear corrections
 - $\Delta x F_3^v \sim 4x(s - c)$
 - $\sin \theta_w$
- * Solving these will provide important information on proton structure
 - Important for search for "New Physics" signals

This is how we will make progress