Process dependent transverse spin asymmetry - understand inclusive hadron production

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Gamberg, Kang, arXiv:1009.1936 ask for latest version if interested

Experiment: Single transverse spin asymmetries (SSAs)

Fermilab E704, STAR, PHENIX, BRAHMS, COMPASS, HERMES, JLAB:



Collinear twist-3 factorization approach:



 $\sigma(p_h, s_\perp) \propto f_{a/A}^{s_\perp}(x) \otimes D_{h/c}(z) \otimes \hat{\sigma}_{\text{parton}}$

- Twist-3 three-parton corrlation functions (PDFs)
- Twist-3 three-parton fragmentation functions



Efremov-Teryaev 82, 84, Qiu-Sterman 91, 98, ... Koike, 02, Kang, Yuan, Zhou 2010



Factorization is expected to hold

Two approaches for inclusive hadron production - II

 Generalized Parton Model (GPM) approach: (assuming factorization)



$$\mathrm{d}\sigma^{\uparrow} = \sum_{a,b,c=q,\bar{q},g} \underbrace{f_{a/p^{\uparrow}}(x_a, \boldsymbol{k}_{\perp a}) \otimes f_{b/p}(x_b, \boldsymbol{k}_{\perp b})}_{\text{single spin effects in TMDs}} \otimes \mathrm{d}\hat{\sigma}^{ab \to cd}(\boldsymbol{k}_{\perp a}, \boldsymbol{k}_{\perp b}) \otimes \underbrace{D_{\pi/c}(z, \boldsymbol{p}_{\perp \pi})}_{\text{single spin effects in TMDs}}$$

M.A., M. Boglione, U. D'Alesio, E. Leader, S. Melis, F. Murgia, A. Prokudin, ... (first proposed by Field-Feynman in unpolarized case)

- Sivers and Collins effect
- TMD factorization is assumed, and no rigorous proof, unlikely to hold
 - TMD factorization is only proved for SIDIS, DY, e+e- (to two hadrons)

Both approaches seem to be successful - I

Collinear twist-3 factorization approach describe data well



Both approaches seem to be successful - II



- Using Sivers functions extracted from HERMES, make predictions for inclusive hadron at RHIC
- Question: Sivers function is process dependent, how can we be sure the Sivers function in $pp^{\uparrow} \rightarrow \pi + X$ is the same as in SIDIS, especially when we know that in DY $pp^{\uparrow} \rightarrow [\gamma^* \rightarrow \ell^+ \ell^-] + X$ is opposite?

Differences between two approaches

 Collinear twist-3 approach takes care of the process-dependence (color flow) of the Sivers function



GPM approach does NOT consider the process-dependence

Process dependence of the Sivers functions

- Gauge links (initial- and final-state interactions) are important for the existence of the Sivers functions
 - Without gauge links, the Sivers function vanishes
 Collins 93
 - With gauge links (generated from initial- and final-state interactions), the Sivers function exists, but non-universal (process-dependent) due to the difference from initial- and final-state interactions



What about inclusive hadron production in pp collisions?

- Both initial- and final-state interactions exist for inclusive hadron productions
 - Sivers function in general can NOT be the same as those in SIDIS, as assumed in current GPM approach



One needs to consider these interactions to determine the proper Sivers function to be used in inclusive hadron production, to have a more consistent picture

How to determine the appropriate Sivers functions

- Lesson from SIDIS and DY processes: one-gluon exchange
 - SIDIS: final-state interaction, using eikonal approximation



$$\bar{u}(p_c)(-ig)\gamma^{-}T^{a}\frac{i(\not p_c - \not k)}{(p_c - k)^2 + i\epsilon} \approx \bar{u}(p_c)\left[\frac{g}{-k^{+} + i\epsilon}T^{a}\right]$$

DY: initial-state interaction



$$\bar{v}(p_b)(-ig)\gamma^{-}T^a \frac{-i(\not p_b + \not k)}{(p_b + k)^2 + i\epsilon} \approx \bar{v}(p_b) \left[\frac{g}{-k^+ (-i\epsilon)}T^a\right]$$

Imaginary part (1st term of gauge link expansion) leads to the sign change

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Do the same for inclusive hadron production

■ Take qq'→qq' as an example:



• One might shift this factor to the hard part function (under this order only) $f_{1T}^{\perp a, \text{SIDIS}} H_{aa' \rightarrow aa'}^U \equiv f_{1T}^{\perp a, \text{SIDIS}} [C_u h_{qq' \rightarrow qq'}] \quad \text{GPM}$

$$f_{1T}^{\perp a,qq' \rightarrow qq'} H_{qq' \rightarrow qq'}^{U} = \frac{C_I + C_{F_c}}{C_u} f_{1T}^{\perp a,\text{SIDIS}} H_{qq' \rightarrow qq'}^{U} = f_{1T}^{\perp a,\text{SIDIS}} \underbrace{C_I h_{qq' \rightarrow qq'} + C_{F_c} h_{qq' \rightarrow qq'}}_{C_I h_{qq' \rightarrow qq'} + C_{F_c} h_{qq' \rightarrow qq'}}$$

Many other channels also contribute

- Do the same for all other channels: $q\bar{q} \rightarrow q\bar{q}, qg \rightarrow qg, qg \rightarrow gq, q\bar{q} \rightarrow gg, \cdots$
- Eventually, we obtain a new (modified) GPM formalism:
 - Contains process-dependence of the Sivers functions

$$E_{h}\frac{d\Delta\sigma}{d^{3}P_{h}} = \frac{\alpha_{s}^{2}}{S}\sum_{a,b,c}\int \frac{dx_{a}}{x_{a}}d^{2}k_{aT}f_{1T}^{\perp a,\text{SIDIS}}(x_{a},k_{aT}^{2})\frac{\epsilon^{k_{aT}S_{A}n\bar{n}}}{M}\int \frac{dx_{b}}{x_{b}}d^{2}k_{bT}f_{b/B}(x_{b},k_{bT}^{2})$$

$$\times \int \frac{dz_{c}}{z_{c}^{2}}D_{h/c}(z_{c})H_{ab\rightarrow c}^{\text{Inc}}(\hat{s},\hat{t},\hat{u})\delta(\hat{s}+\hat{t}+\hat{u})$$

$$H_{ab\rightarrow c}^{U}(\hat{s},\hat{t},\hat{u}) \quad \text{GPM}$$

 $H_{ab \to c}^{\mathrm{Inc}}(\hat{s}, \hat{t}, \hat{u}) = H_{ab \to c}^{\mathrm{Inc}-\mathrm{I}}(\hat{s}, \hat{t}, \hat{u}) + H_{ab \to c}^{\mathrm{Inc}-\mathrm{F}}(\hat{s}, \hat{t}, \hat{u})$

initial-state final-state

- Hard-part functions (both initial- and final-) are exactly the same as those in collinear twist-3 approach in terms of Mandelstam variables $\hat{s}, \hat{t}, \hat{u}$
- Collinear twist-3: parton momenta are collinear, so are $\hat{s}, \hat{t}, \hat{u}$
- GPM: parton momenta depend on kt, so are $\hat{s}, \hat{t}, \hat{u}$

Even though it is claimed sometimes that GPM is a leading twist formalism, it is NOT

$$E_{h}\frac{d\Delta\sigma}{d^{3}P_{h}} = \frac{\alpha_{s}^{2}}{S}\sum_{a,b,c}\int \frac{dx_{a}}{x_{a}}d^{2}k_{aT}f_{1T}^{\perp a,\text{SIDIS}}(x_{a},k_{aT}^{2}) \underbrace{\underbrace{\epsilon^{k_{aT}S_{A}n\bar{n}}}_{M}}_{M}\int \frac{dx_{b}}{x_{b}}d^{2}k_{bT}f_{b/B}(x_{b},k_{bT}^{2})$$
$$\times \int \frac{dz_{c}}{z_{c}^{2}}D_{h/c}(z_{c})H_{ab\rightarrow c}^{\text{Inc}}(\hat{s},\hat{t},\hat{u})\delta(\hat{s}+\hat{t}+\hat{u})$$

- Because of the linear kt from Sivers function definition, one needs to pick up another linear kt from the expansion of the hard-part function, thus it is the ktexpansion term contributes
- One has to keep the kt-dependence in the hard-part functions, otherwise the integral vanishes (no SSAs can be generated from this approach)
- This is not TMD factorization formalism (no TMD factorization established for inclusive hadron production)
 - Typically TMD factorization applies for processes with two scales: SIDIS, DY
 - Typically hard-part functions do NOT contain any soft scale, like kt in our case

What is the first kt-expansion

$$\begin{split} E_{h}\frac{d\Delta\sigma}{d^{3}P_{h}} &= \frac{\alpha_{s}^{2}}{S}\sum_{a,b,c}\int\frac{dx_{a}}{x_{a}}d^{2}k_{aT}f_{1T}^{\perp a,\text{SIDIS}}(x_{a},k_{aT}^{2})\frac{\epsilon^{k_{aT}S_{A}n\bar{n}}}{M}\int\frac{dx_{b}}{x_{b}}d^{2}k_{bT}f_{b/B}(x_{b},k_{bT}^{2})\\ &\times\int\frac{dz_{c}}{z_{c}^{2}}D_{h/c}(z_{c})H_{ab\rightarrow c}^{\text{Inc}}(\hat{s},\hat{t},\hat{u})\delta(\hat{s}+\hat{t}+\hat{u})\\ p_{a}^{\mu}\approx x_{a}P_{A}^{\mu}+k_{aT} \qquad p_{b}^{\mu}\approx x_{b}P_{B}^{\mu} \\ \delta(\hat{s}+\hat{t}+\hat{u}) &= \frac{1}{x_{b}S+T/z_{c}}\delta\left(x_{a}-x-\frac{2P_{hT}\cdot k_{aT}}{z_{c}x_{b}S+T}\right) \quad \text{where,} \quad x_{a}=x+\frac{2P_{hT}\cdot k_{aT}}{z_{c}x_{b}S+T}\\ \text{no kt-dependence} \end{split}$$

• $\tilde{s}, \tilde{t}, \tilde{u}$ no kt-dependence

$$\hat{s} = \tilde{s} - \frac{\tilde{s}}{\tilde{u}} 2P_{hT} \cdot k_{aT}/z_c, \qquad \hat{t} = \tilde{t} + \frac{\tilde{s}}{\tilde{u}} 2P_{hT} \cdot k_{aT}/z_c, \qquad \hat{u} = \tilde{u}$$

Hope modified GPM is a reasonable approximation?! - II

The relation between twist-3 correlation function T_F(x, x) and Sivers function

$$T_{a,F}(x,x) = -\frac{1}{M} \int d^2 k_{aT} |\vec{k}_{aT}|^2 f_{1T}^{\perp a,\text{SIDIS}}(x,k_{aT}^2)$$

Finally, the first term in kt-expansion

$$\begin{split} E_{h} \frac{d\Delta\sigma^{(a)}}{d^{3}P_{h}} : & \text{exactly the same as the collinear twist-3 formalism} \\ \frac{\alpha_{s}^{2}}{S} \sum_{a,b,c} \int \frac{dz_{c}}{z_{c}^{2}} D_{h/c}(z_{c}) \frac{\epsilon^{P_{hT}S_{A}n\bar{n}}}{z_{c}\tilde{u}} \frac{1}{x} \left[T_{a,F}(x,x) - x\frac{d}{dx}T_{a,F}(x,x) \right] \int \frac{dx_{b}}{x_{b}} f_{b/B}(x_{b}) H_{ab\rightarrow c}^{\text{Inc}}(\tilde{s},\tilde{t},\tilde{u}) \frac{1}{x_{b}S + T/z_{c}} \\ E_{h} \frac{d\Delta\sigma^{(b)}}{d^{3}P_{h}} : & \text{an extra term, which is proportional to the non-derivative term} \\ \frac{\alpha_{s}^{2}}{S} \sum_{a,b,c} \int \frac{dz_{c}}{z_{c}^{2}} D_{h/c}(z_{c}) \frac{\epsilon^{P_{hT}S_{A}n\bar{n}}}{z_{c}\tilde{u}} \frac{1}{x} T_{a,F}(x,x) \int \frac{dx_{b}}{x_{b}} f_{b/B}(x_{b}) \left[-\tilde{s}\frac{\partial}{\partial\tilde{s}} H_{ab\rightarrow c}^{\text{Inc}}(\tilde{s},-\tilde{s}-\tilde{u},\tilde{u}) \right] \frac{1}{x_{b}S + T/z_{c}} \end{split}$$

Since the derivative term is dominant contribution in forward region, the extra term should be small numerically, thus a reasonable approximation?!

Numerical estimates - I: GPM .vs. Modified GPM

Using the slightly earlier Sivers function parameterizations

Anselmino, et.al., PRD, 2005



- The predictions of modified GPM are almost opposite to those from GPM
- With Sivers effect alone, one cannot describe the data any more
- To compare with inclusive pion data, one also needs to add Collins effect
- Predictions for direct photon is the same between modified GPM and twist-3

Using the latest Sivers functions

Anselmino, et.al., EPJA, 2009



- The latest Sivers functions extracted from SIDIS generate very small asymmetry
- New global fitting is on the way
- To compare with inclusive pion data, one also needs to add Collins effect

- For direct photon production, the dominant channel at forward direction is $qg \rightarrow \gamma q$
 - Without initial-state interaction

$$H^U_{qg \to \gamma q} = \frac{1}{N_c} e_q^2 \left[-\frac{\hat{t}}{\hat{s}} - \frac{\hat{s}}{\hat{t}} \right]$$

With initial-state interaction

$$H_{qg \to \gamma q}^{\text{Inc}} = \Theta_{N_c}^{N_c} e_q^2 \left[-\frac{\hat{t}}{\hat{s}} - \frac{\hat{s}}{\hat{t}} \right]$$



- For inclusive pion production, the dominant channel at forward direction is qg→qg
 - Without initial- and final-state interactions

$$H^U_{qg \to qg} \to \frac{2\hat{s}^2}{\hat{t}^2}$$

With both initial- and final-state interactions

$$H_{qg \to qg}^{\text{Inc}} = H_{qg \to qg}^{\text{Inc}-\text{I}} + H_{qg \to qg}^{\text{Inc}-\text{F}} \to \bigcirc \frac{N_c^2 + 2}{N_c^2 - 1} \frac{\hat{s}^2}{\hat{t}^2}$$



Some comments

- There is no TMD factorization for GPM or our modified GPM approaches, use it with caution
- GPM does not take into account the process-dependence of the Sivers function, it is only a nice intuitive picture, which might be used for illustration only
- Modified GPM contains the process-dependence of the Sivers function to some degree (only under one-gluon exchange), numerically seems close to the well-established collinear twist-3 formalism, should be used if one wants to study the SSAs within GPM framework
- Modified GPM predicts same sign as the collinear twist-3 formalism, but the conventional GPM has opposite predictions, thus direct photon might be a very good channel to test the associated initial color interactions
- Since these process dependence has the same origin as the sign change between SIDIS and DY, we hope to have DY measurements as soon as possible (a much cleaner channel, TMD factorization is proved, no final-state interactions, ...)

Thank you